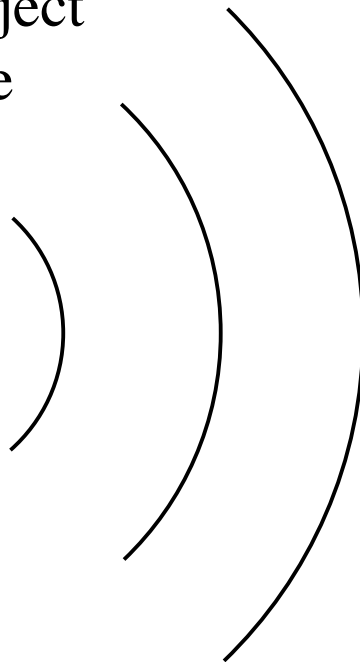


Optical  
System

**Media** – **homogeneous**  
– **isotropic**

Real object  
space

$O$

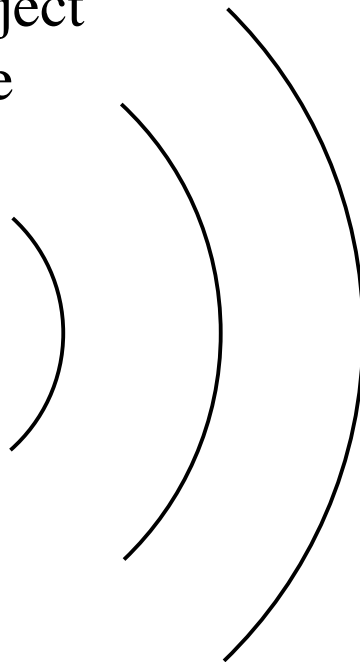


Optical  
System

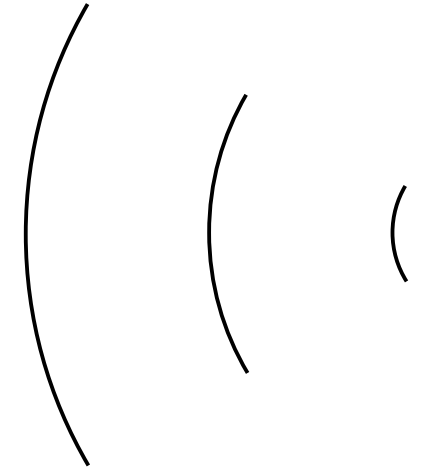


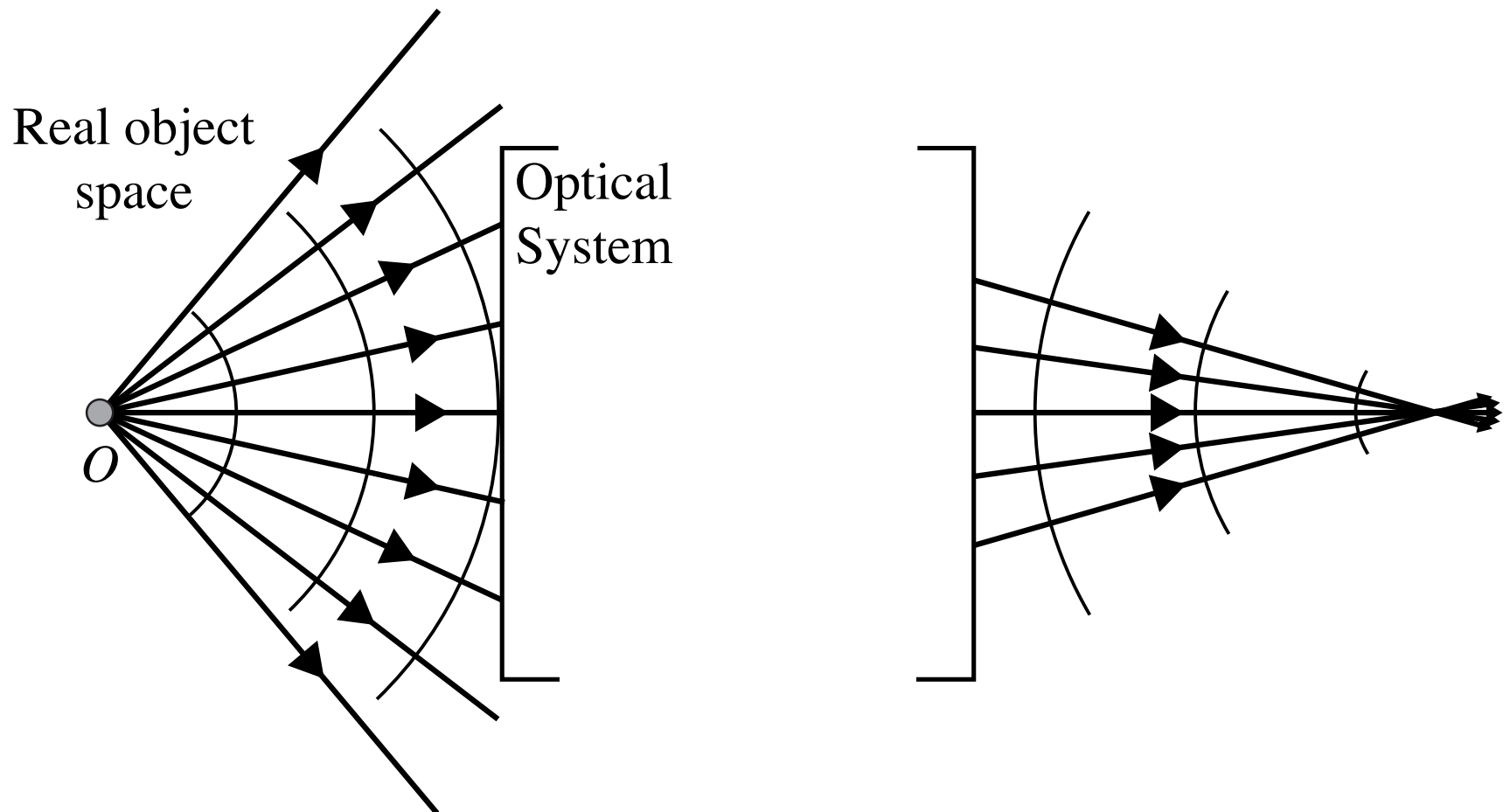
Real object  
space

$O$

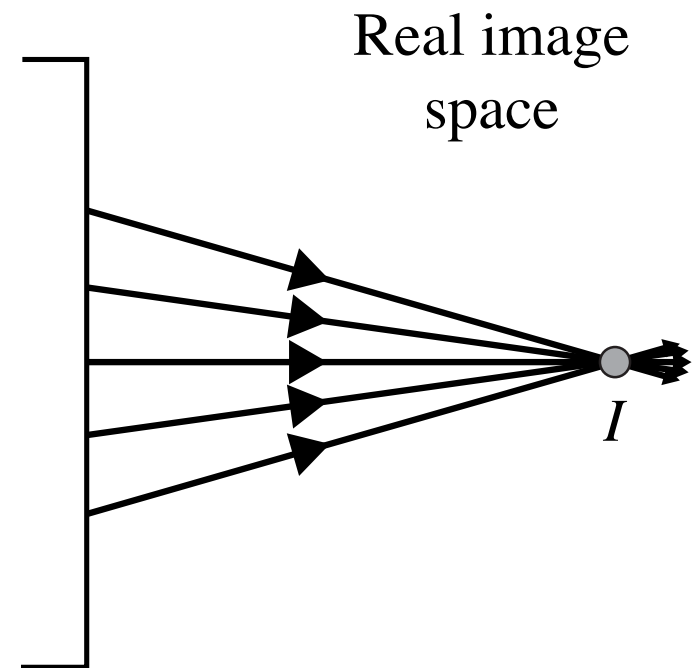
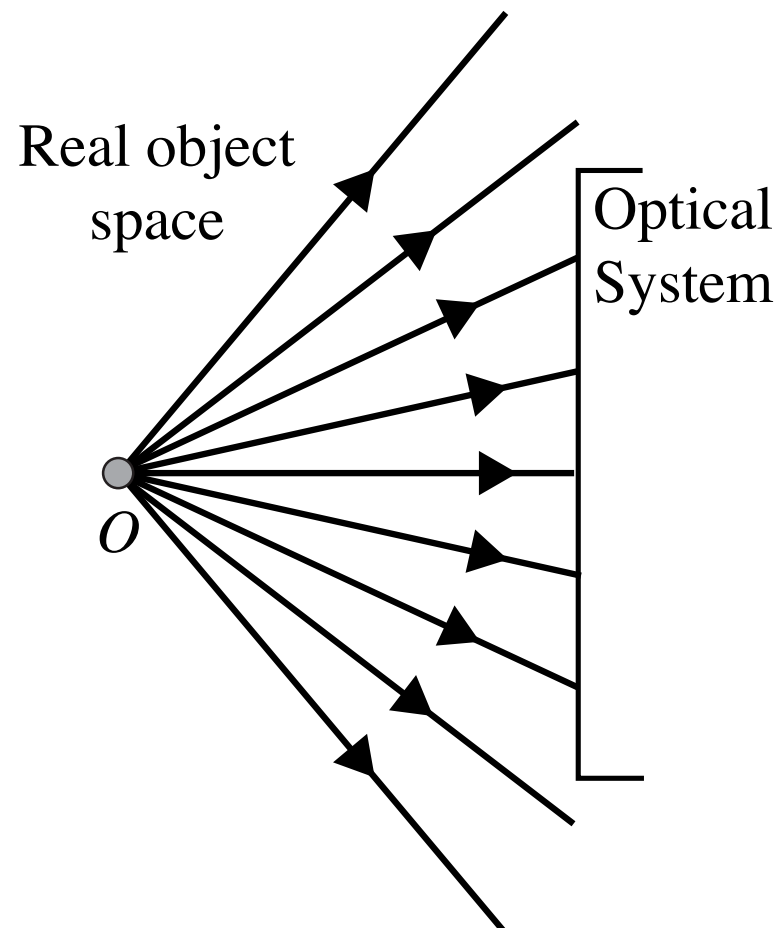


Optical  
System

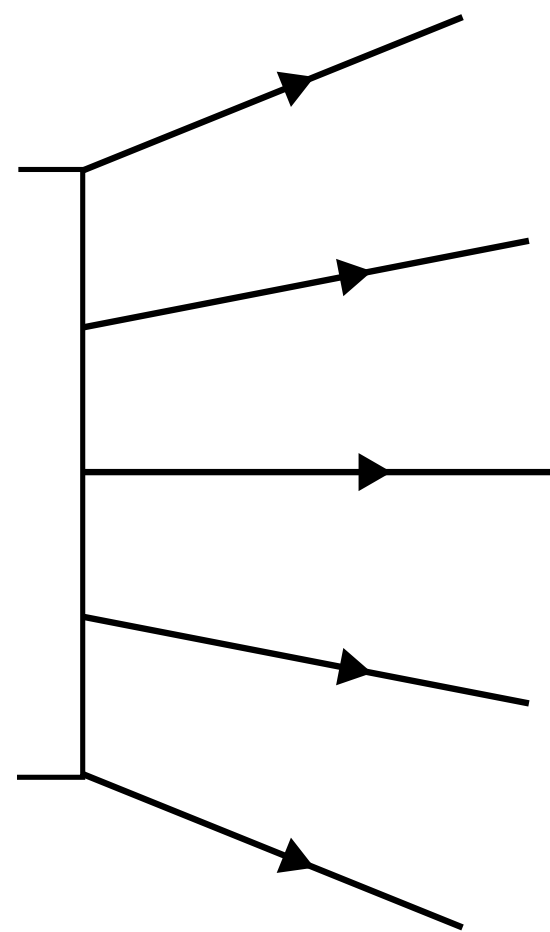
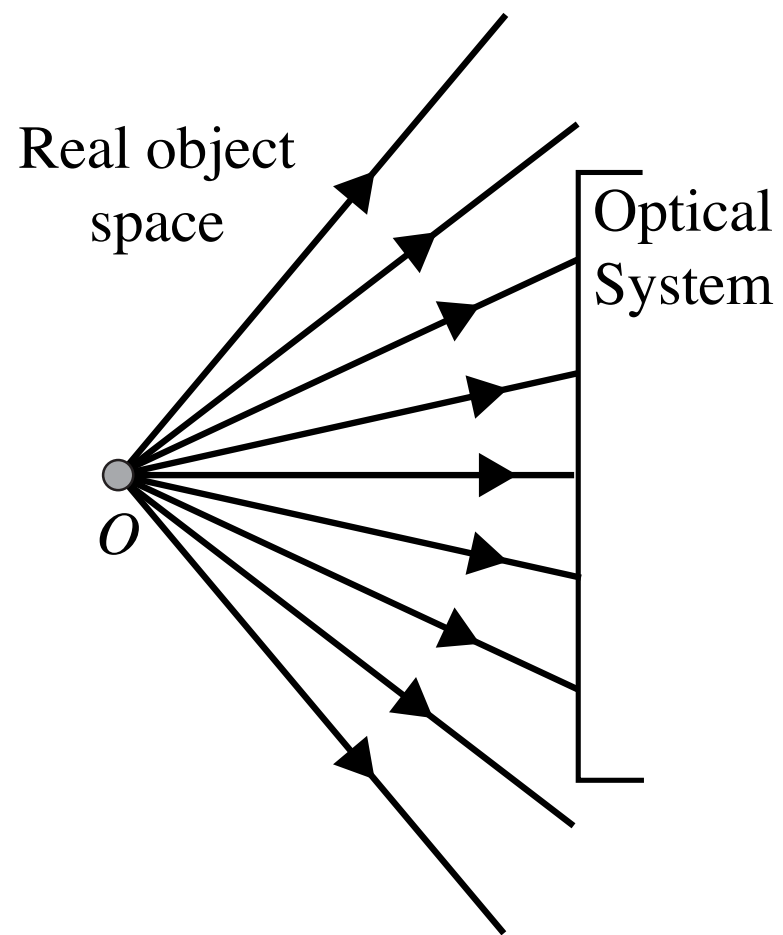


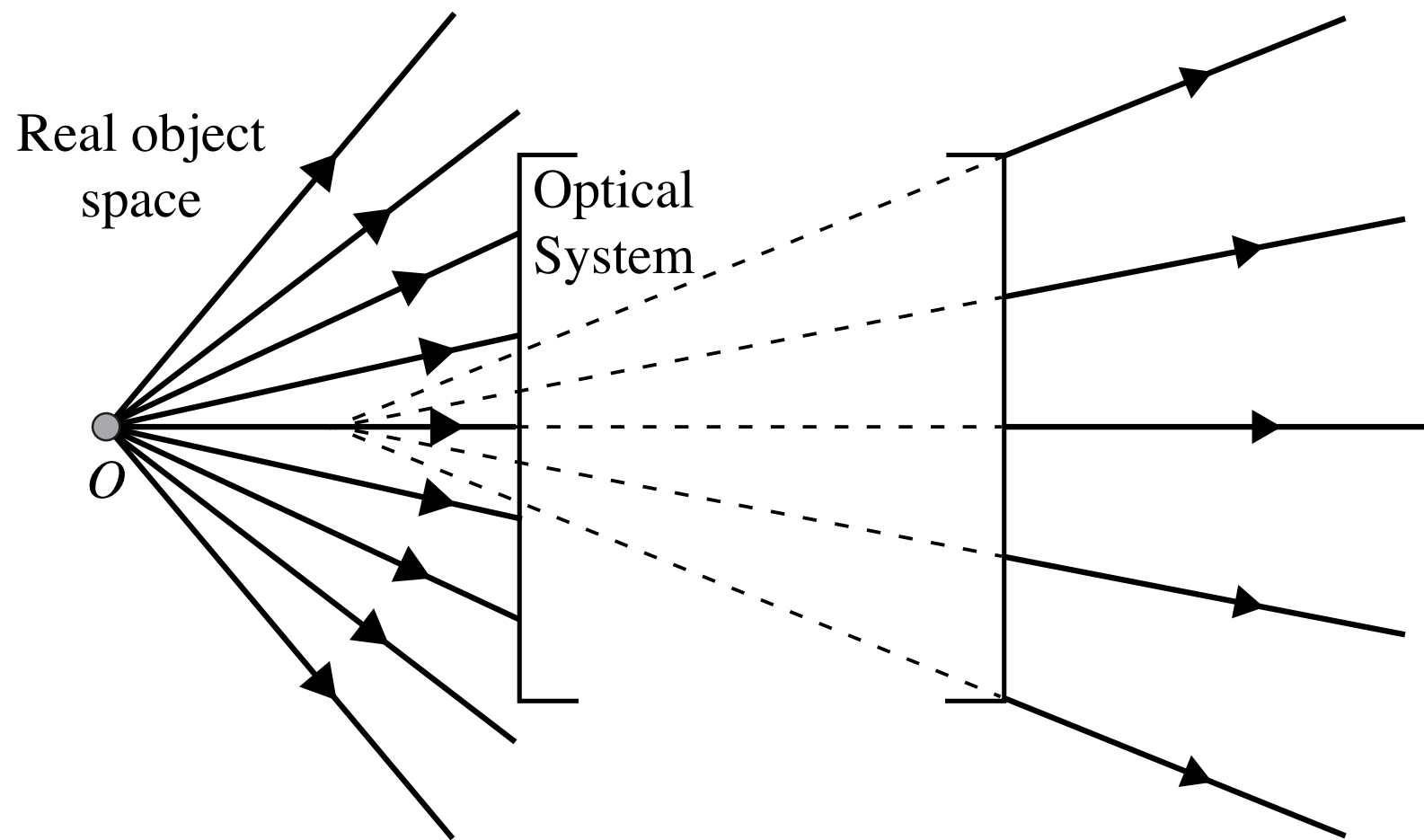


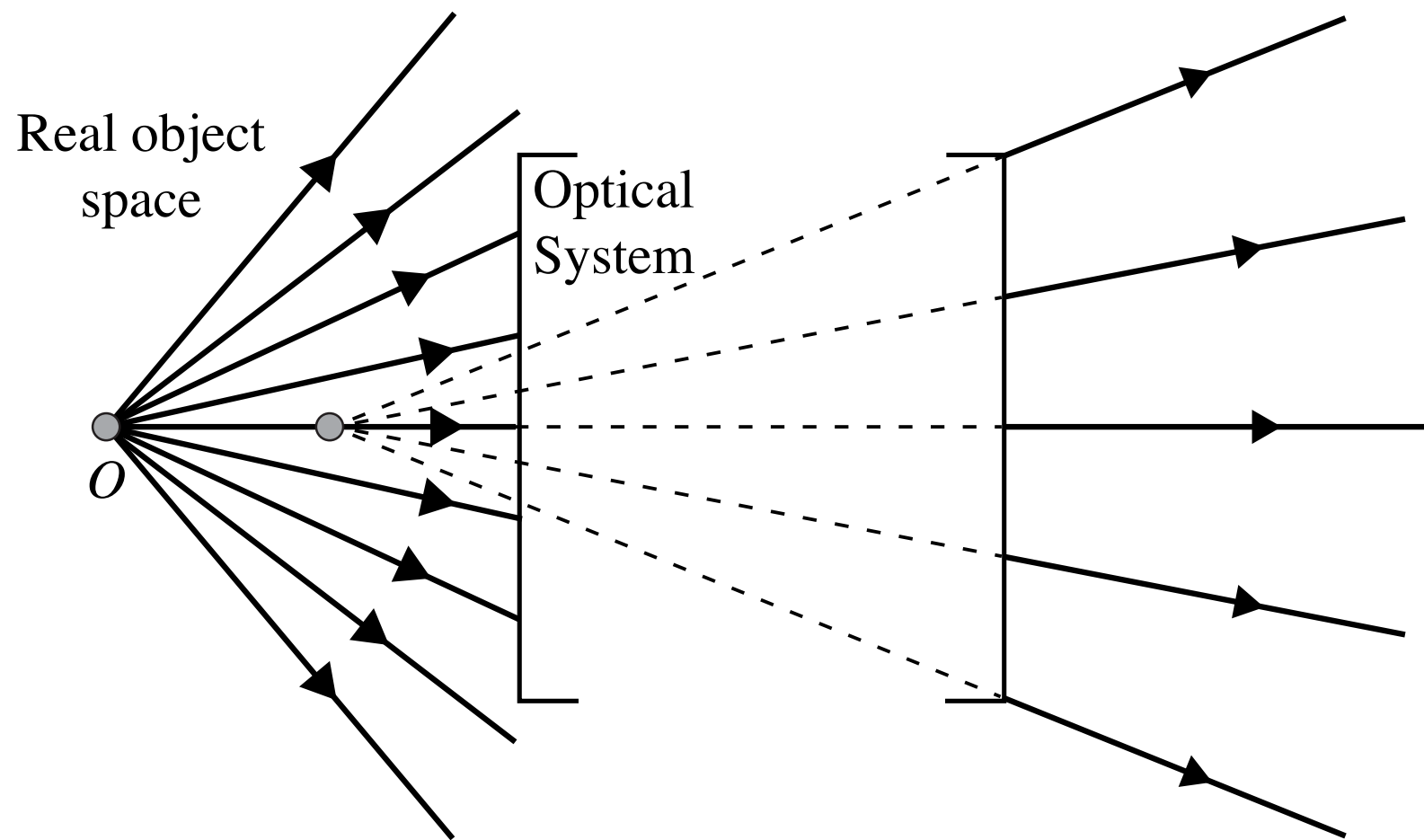
**Isochronous** – each ray has same transit time.  
(Fermat's principle)



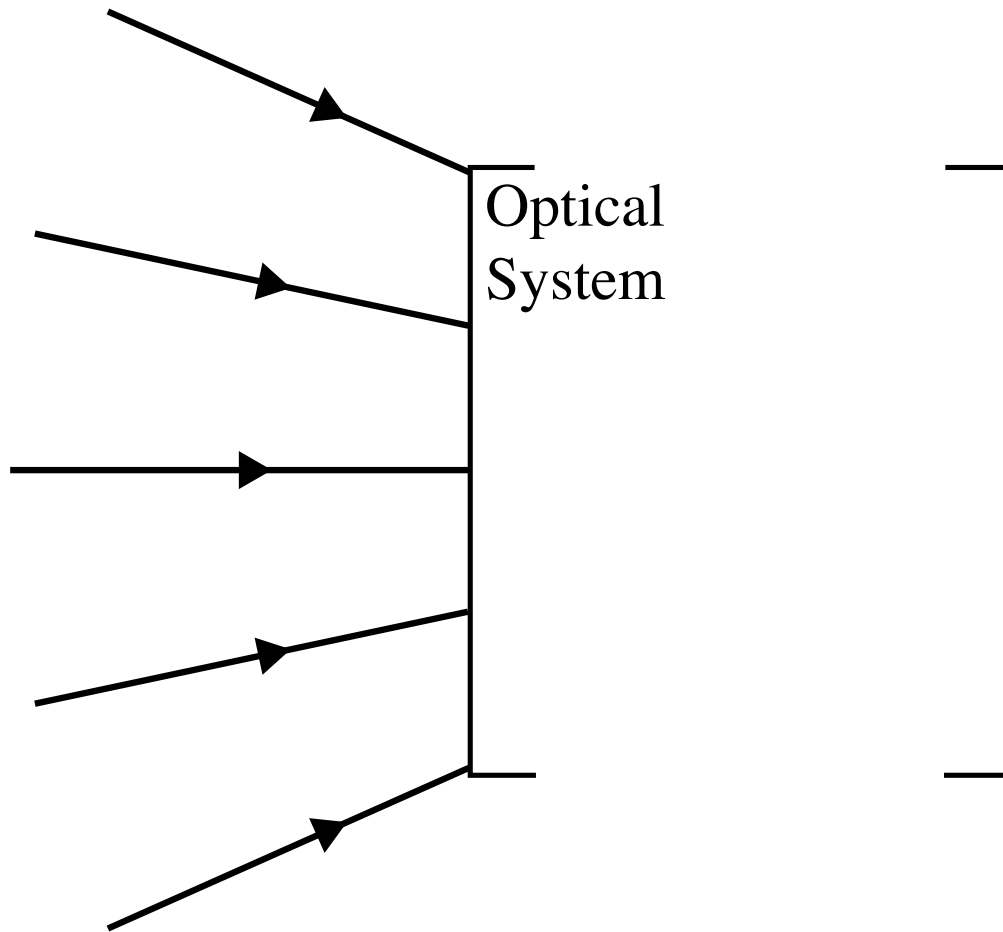
$O$  and  $I$  are **conjugate** points.  
(principle of reversibility)

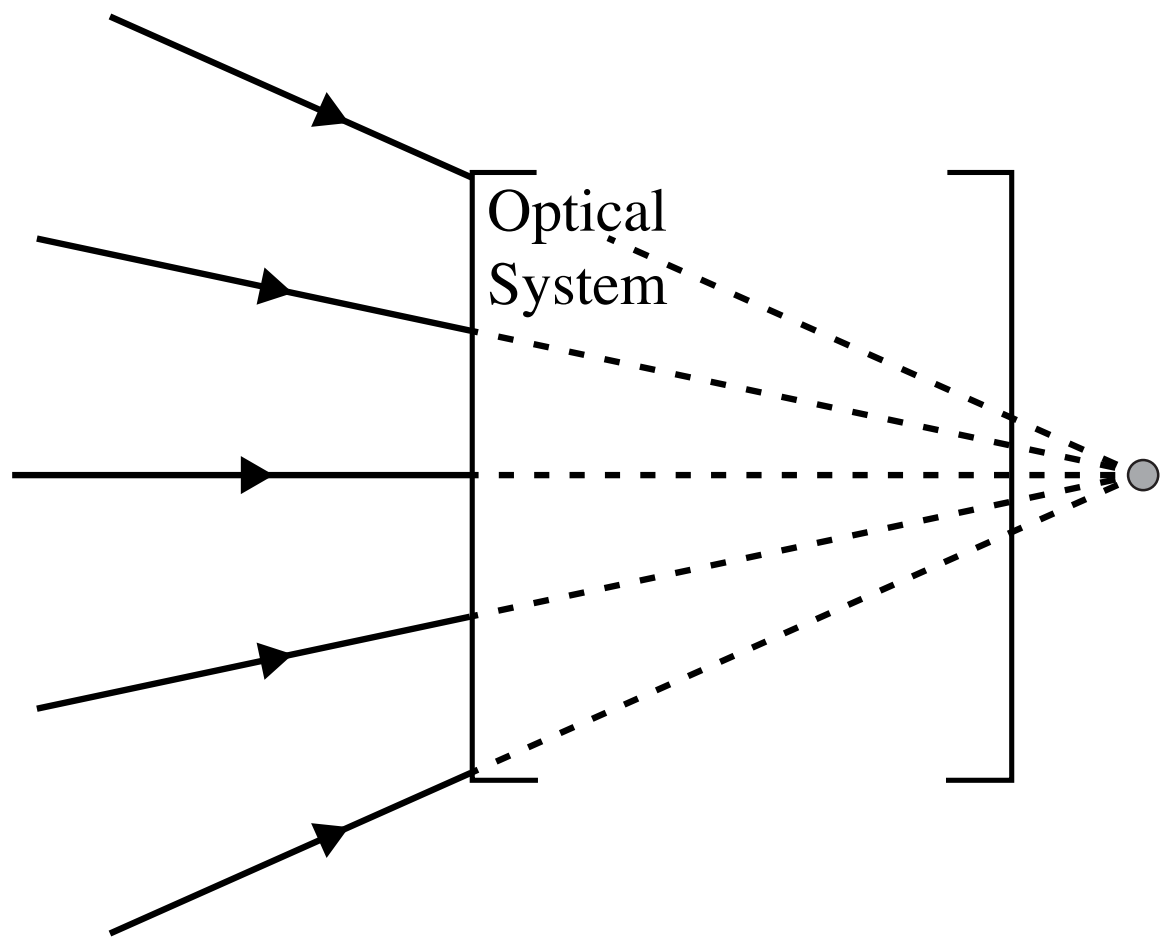




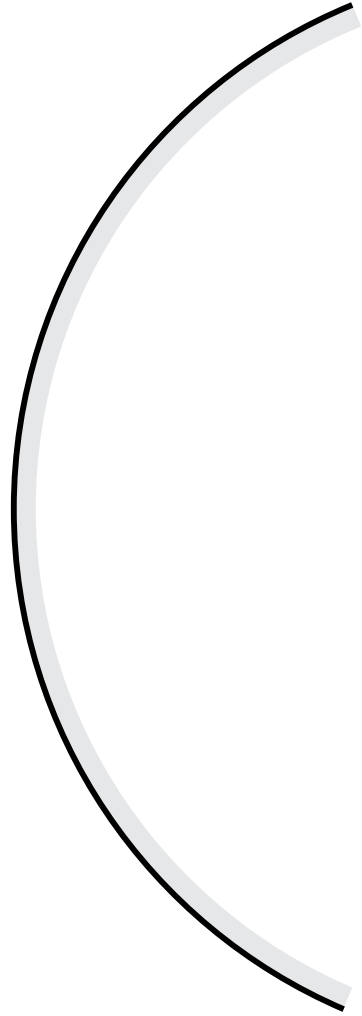




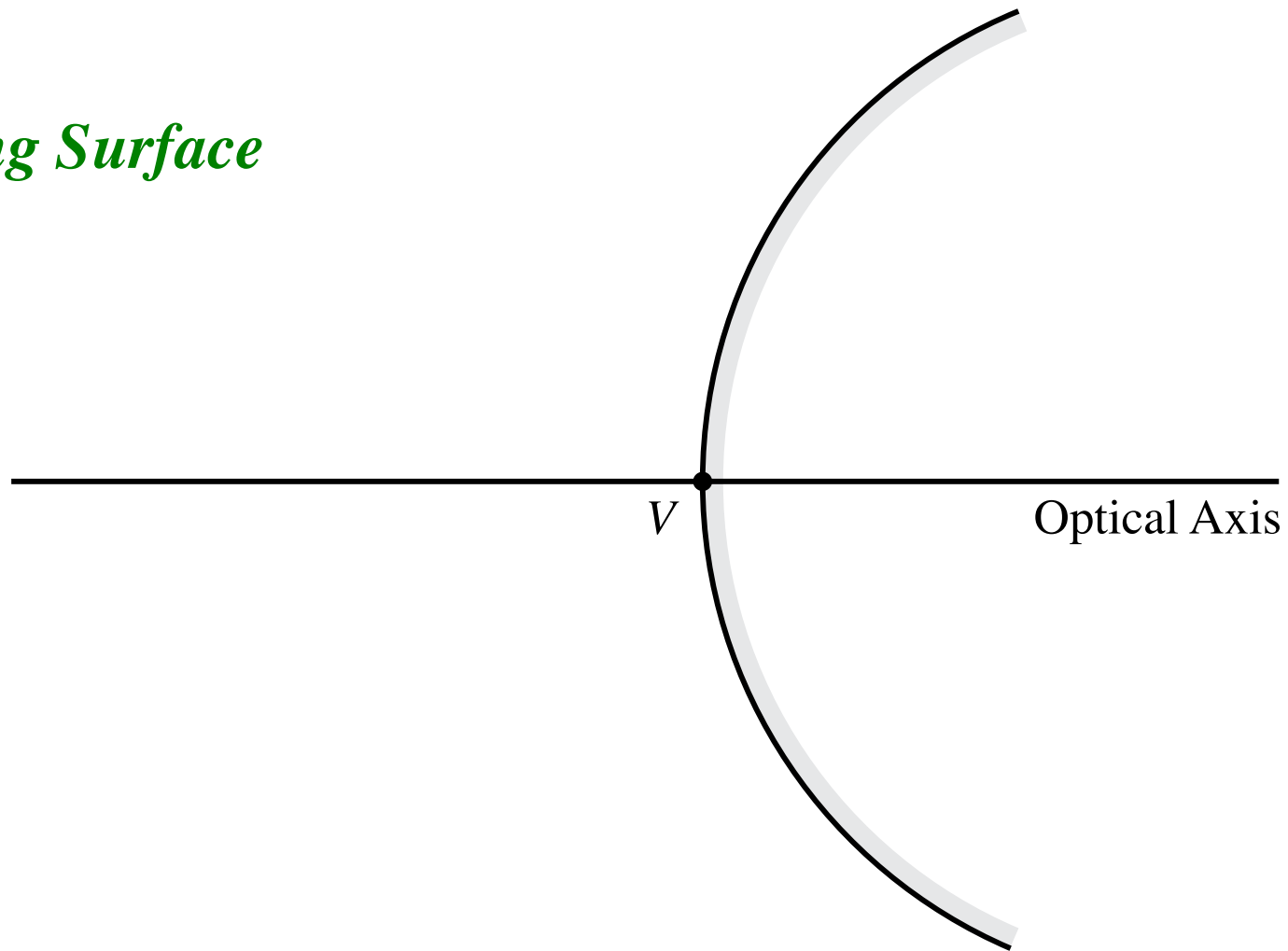




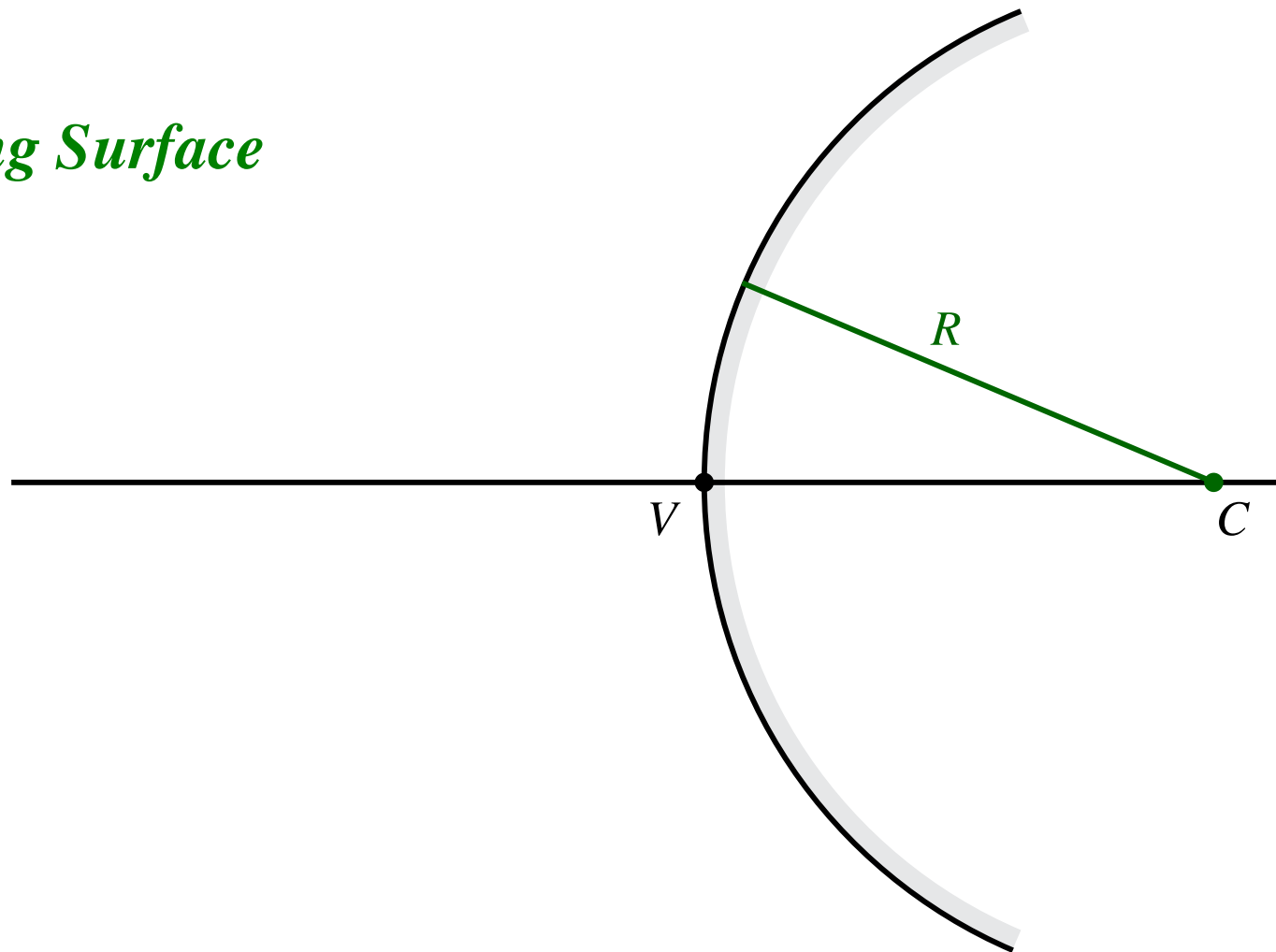
## *Convex Reflecting Surface*



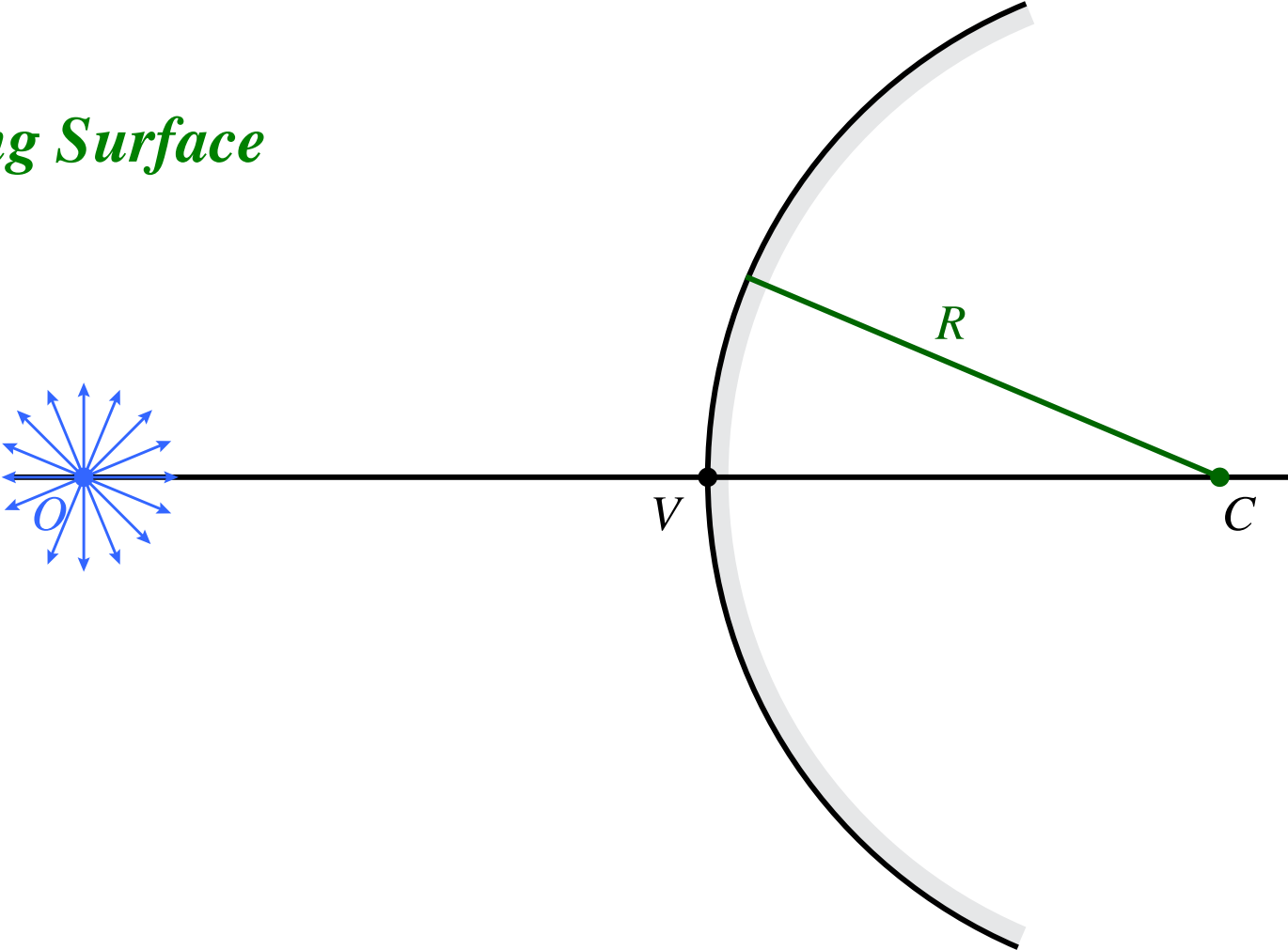
*Convex Reflecting Surface*



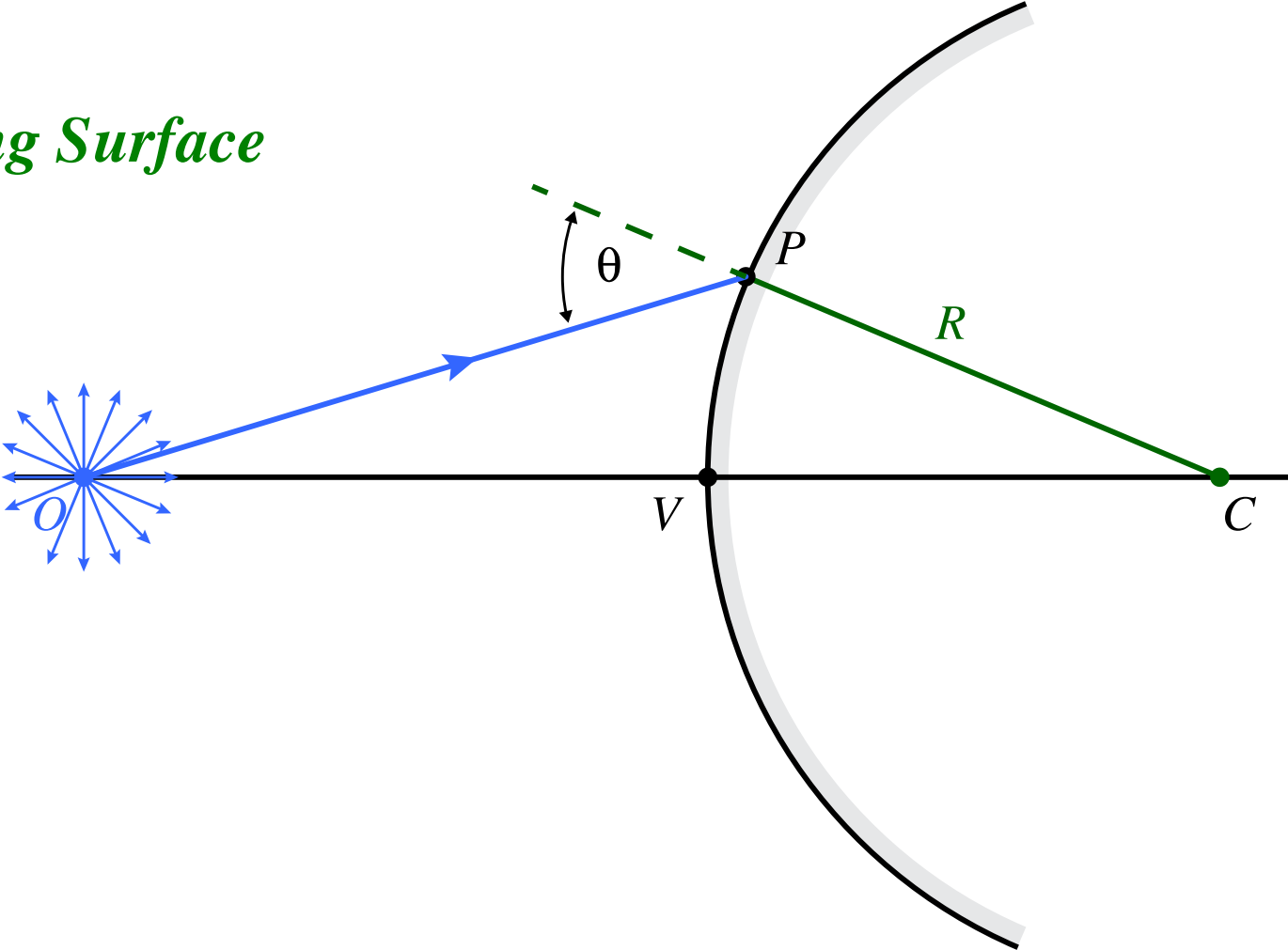
# *Convex Reflecting Surface*



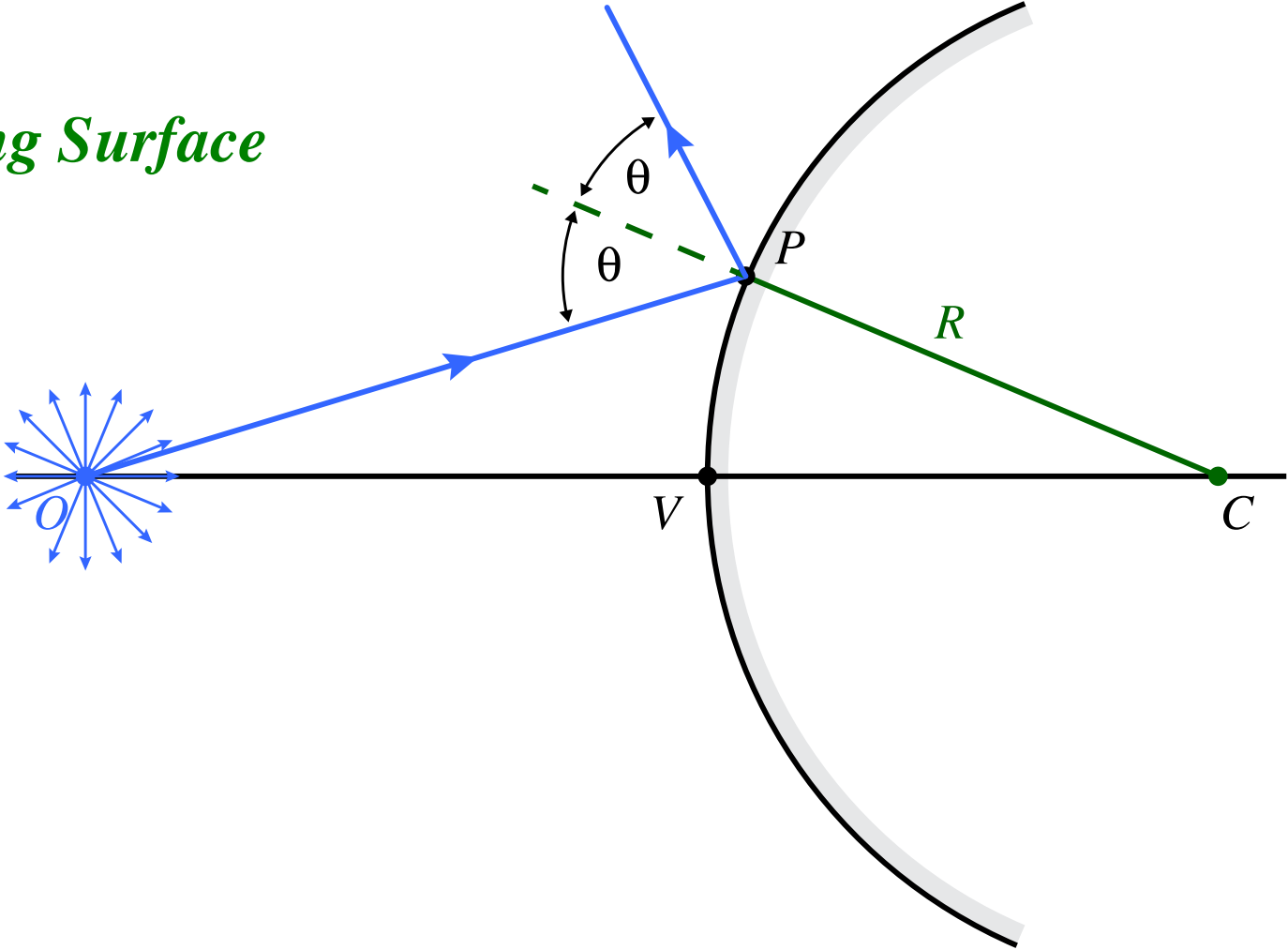
*Convex Reflecting Surface*



*Convex Reflecting Surface*

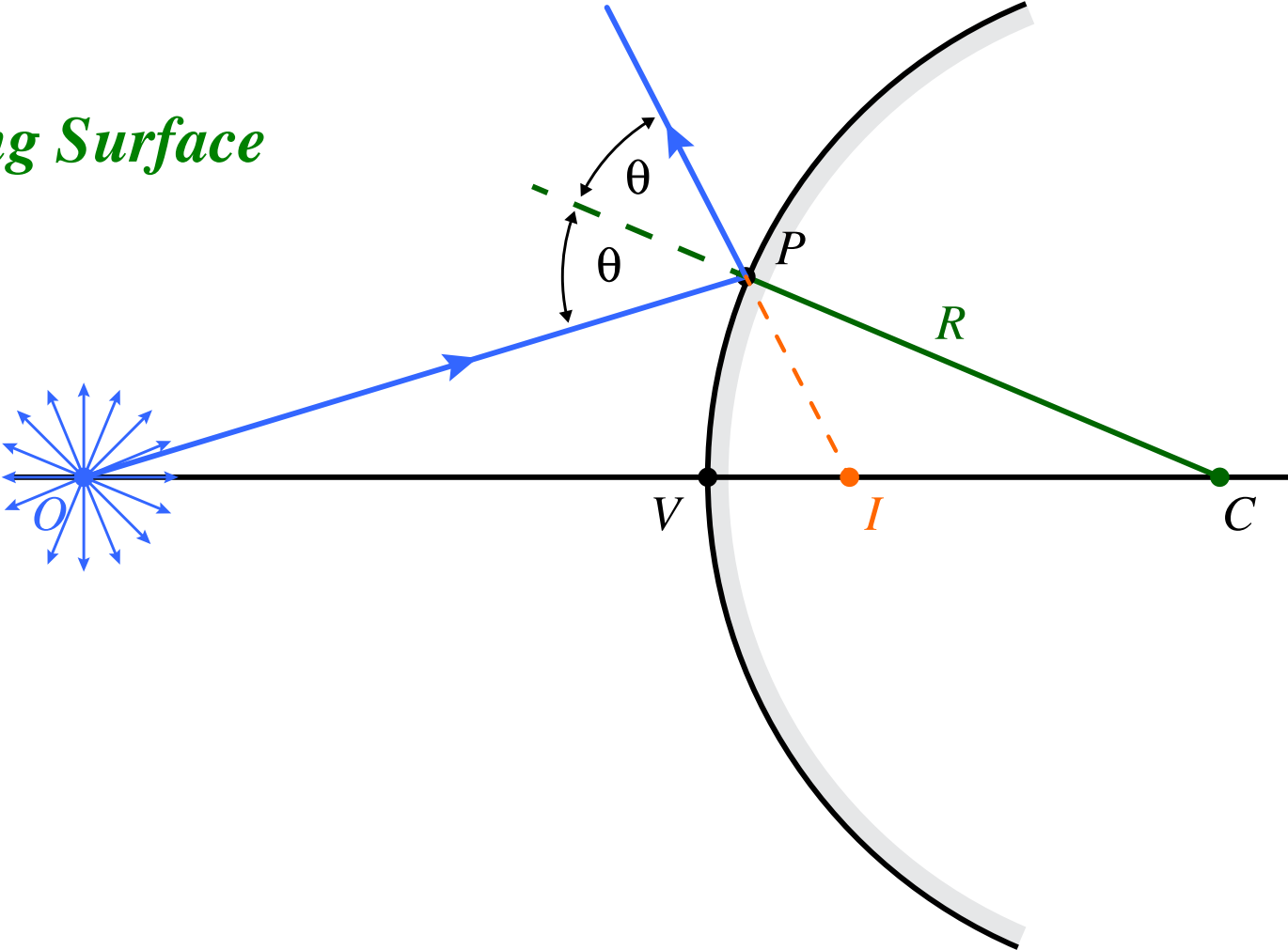


*Convex Reflecting Surface*

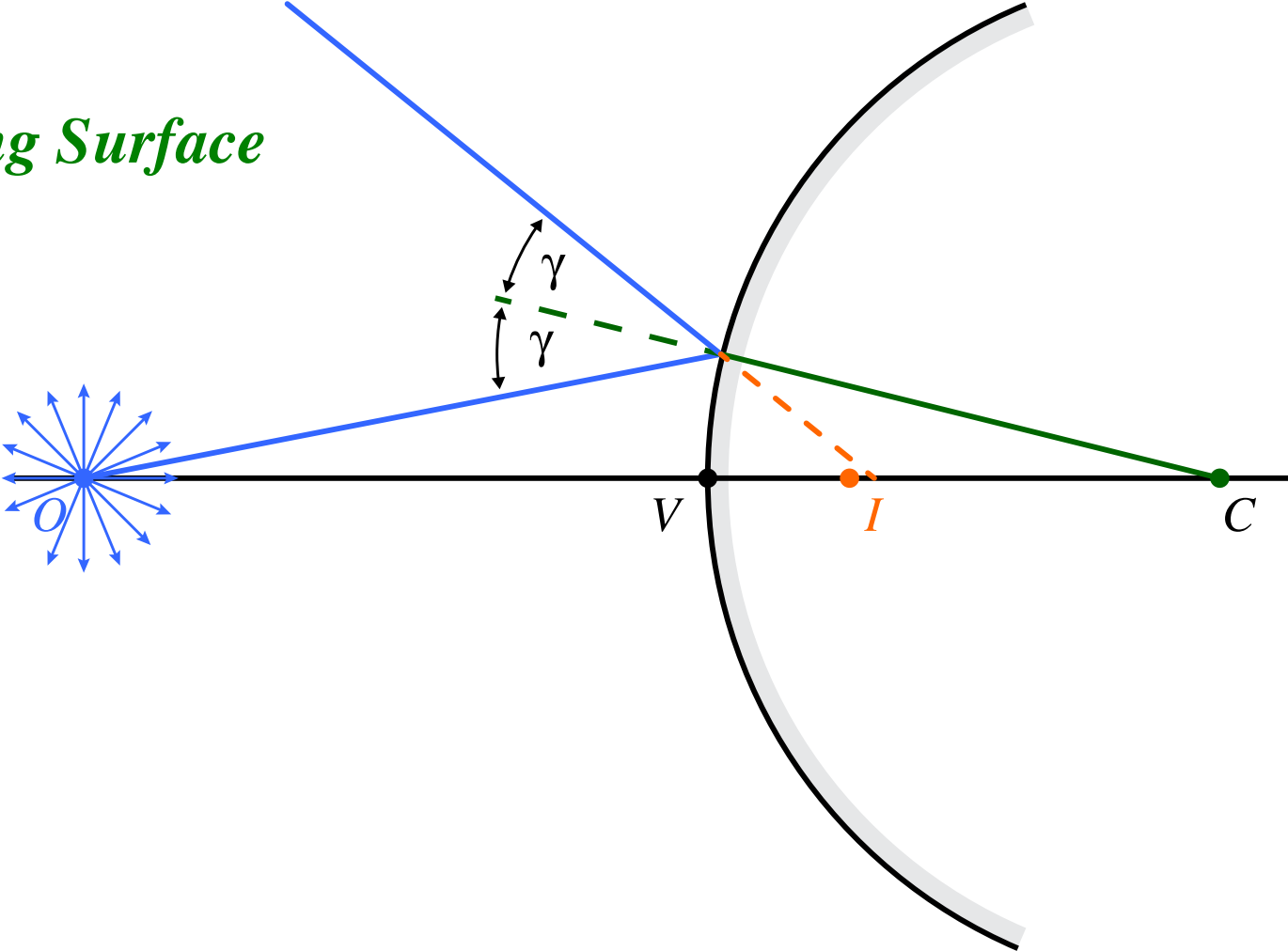




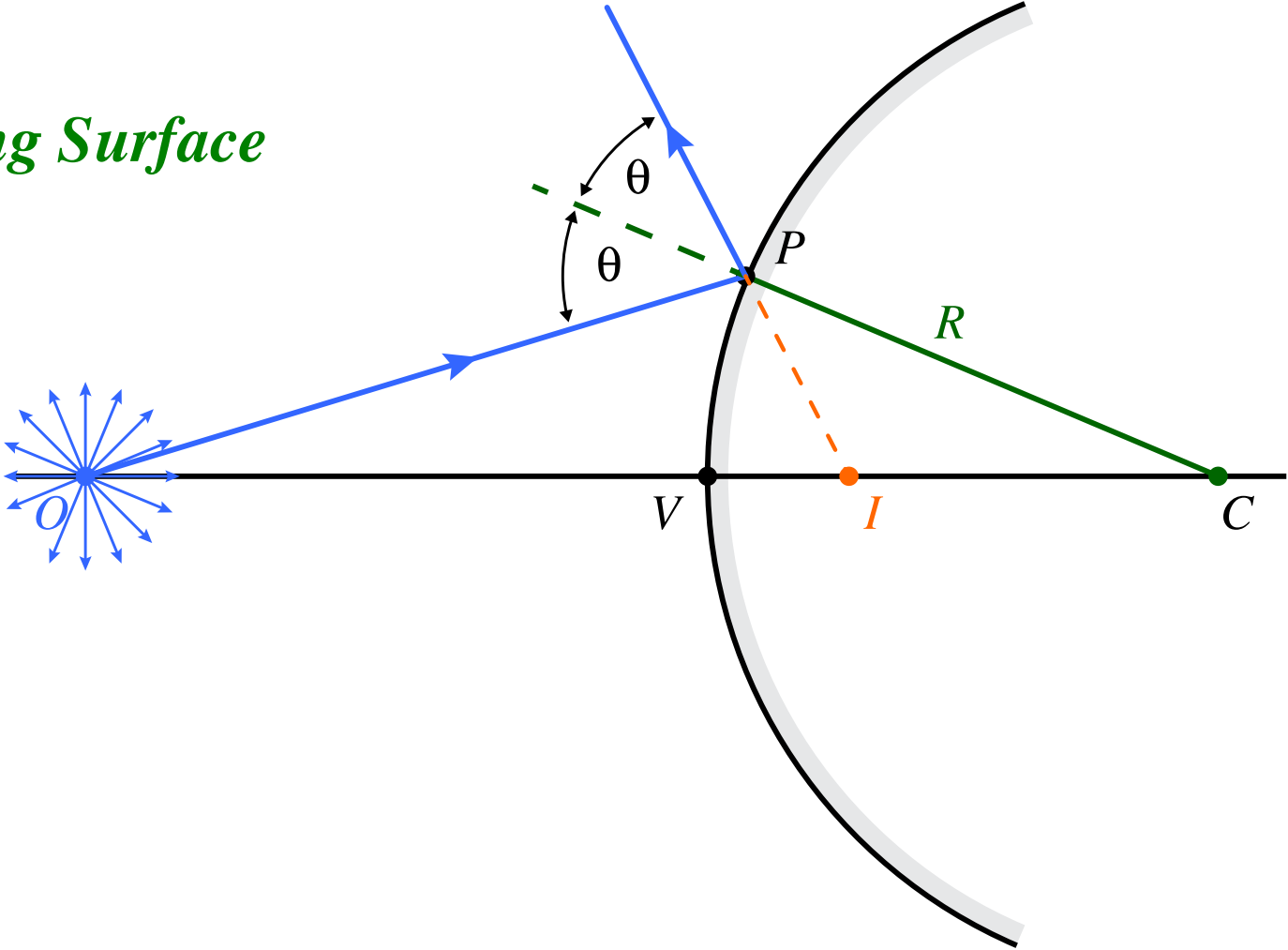
*Convex Reflecting Surface*



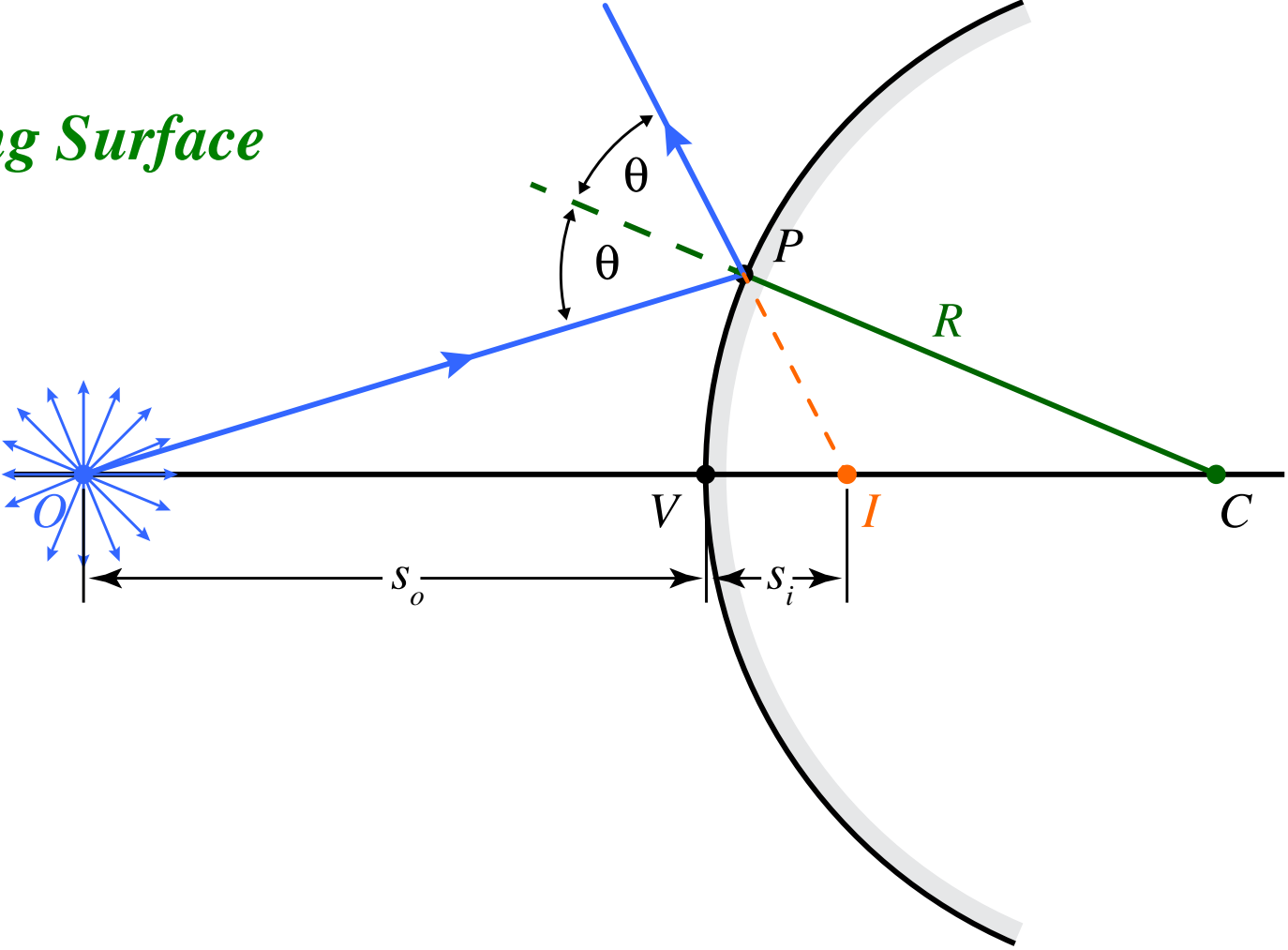
*Convex Reflecting Surface*



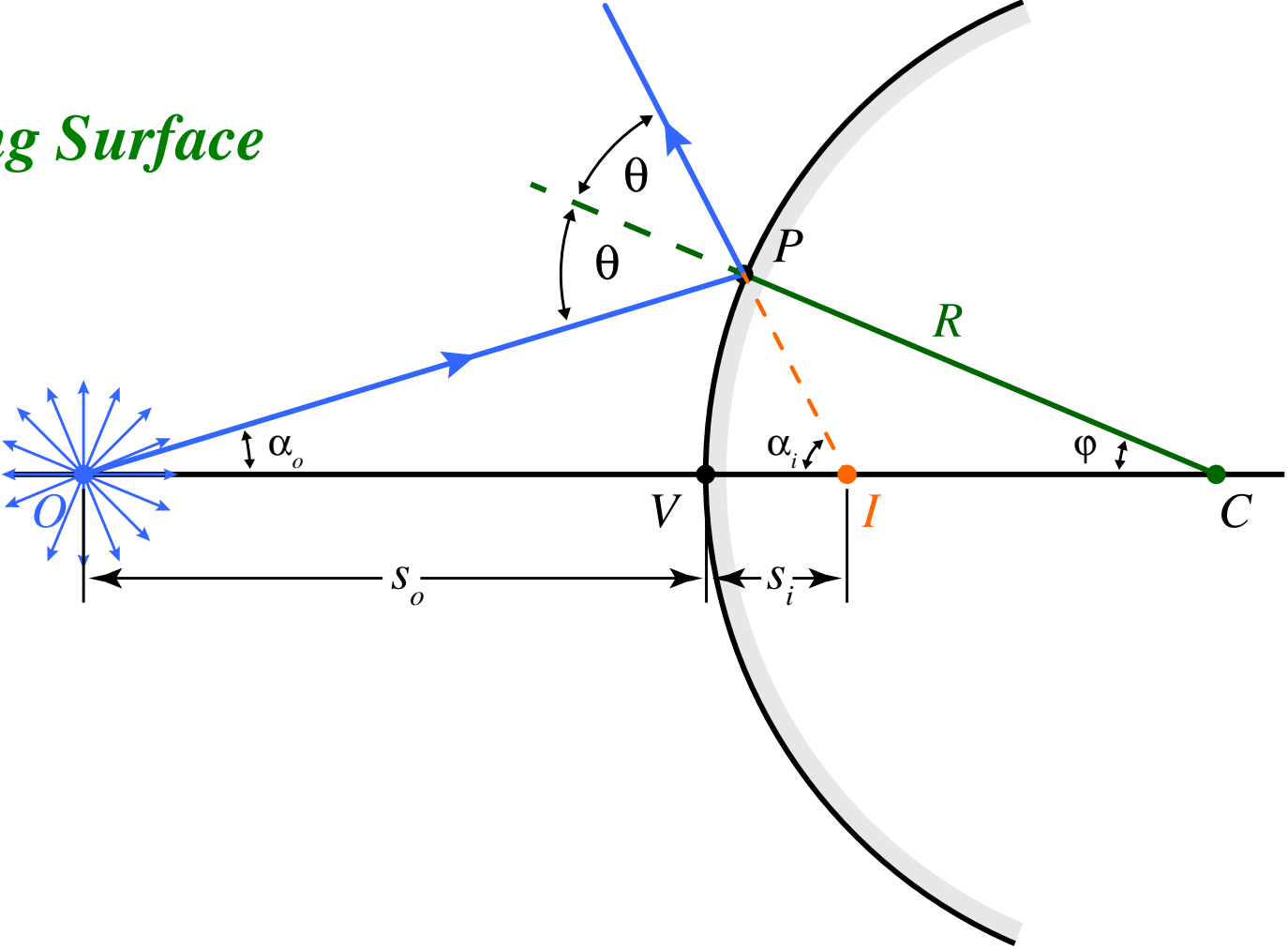
*Convex Reflecting Surface*



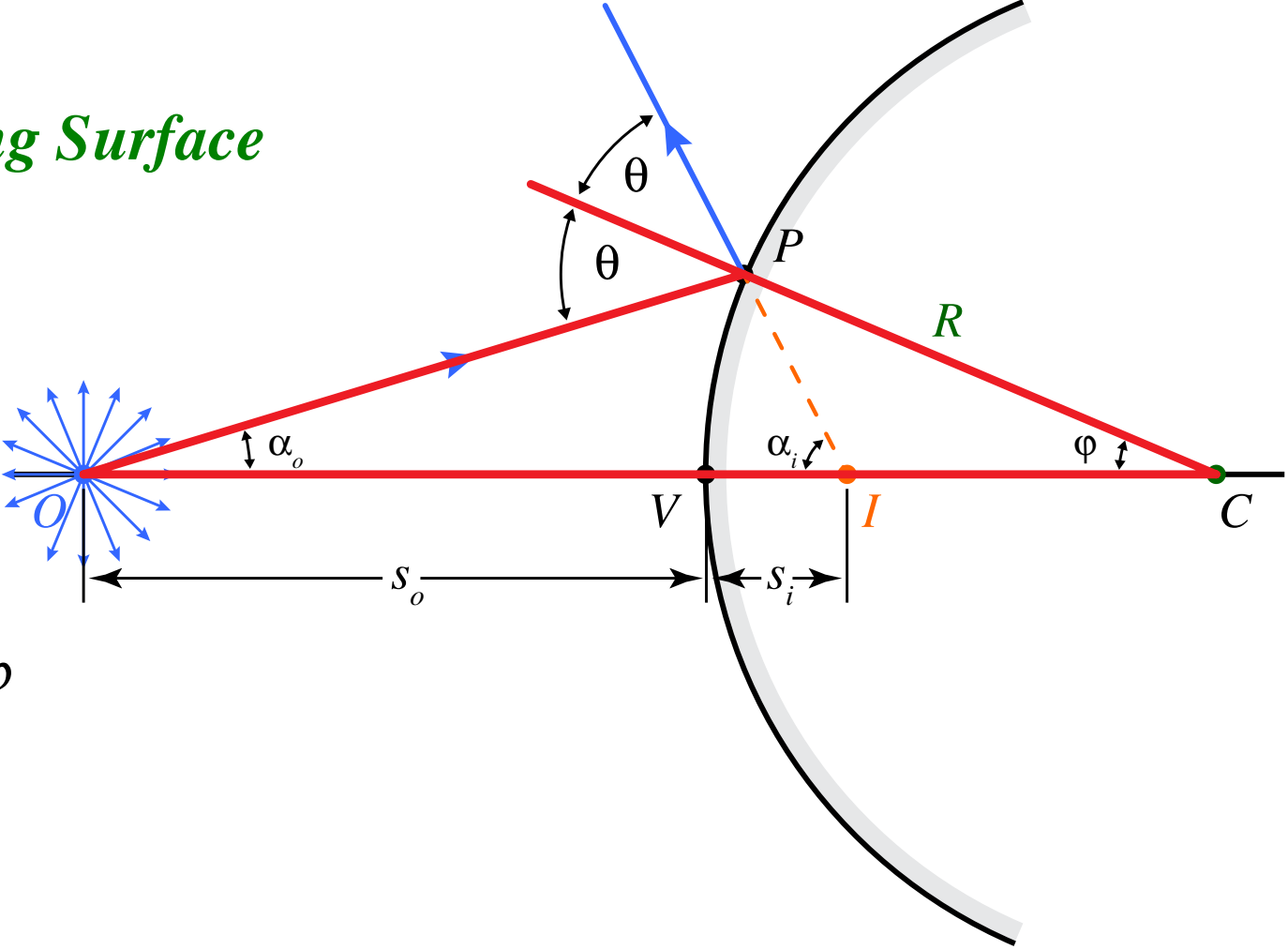
*Convex Reflecting Surface*



*Convex Reflecting Surface*

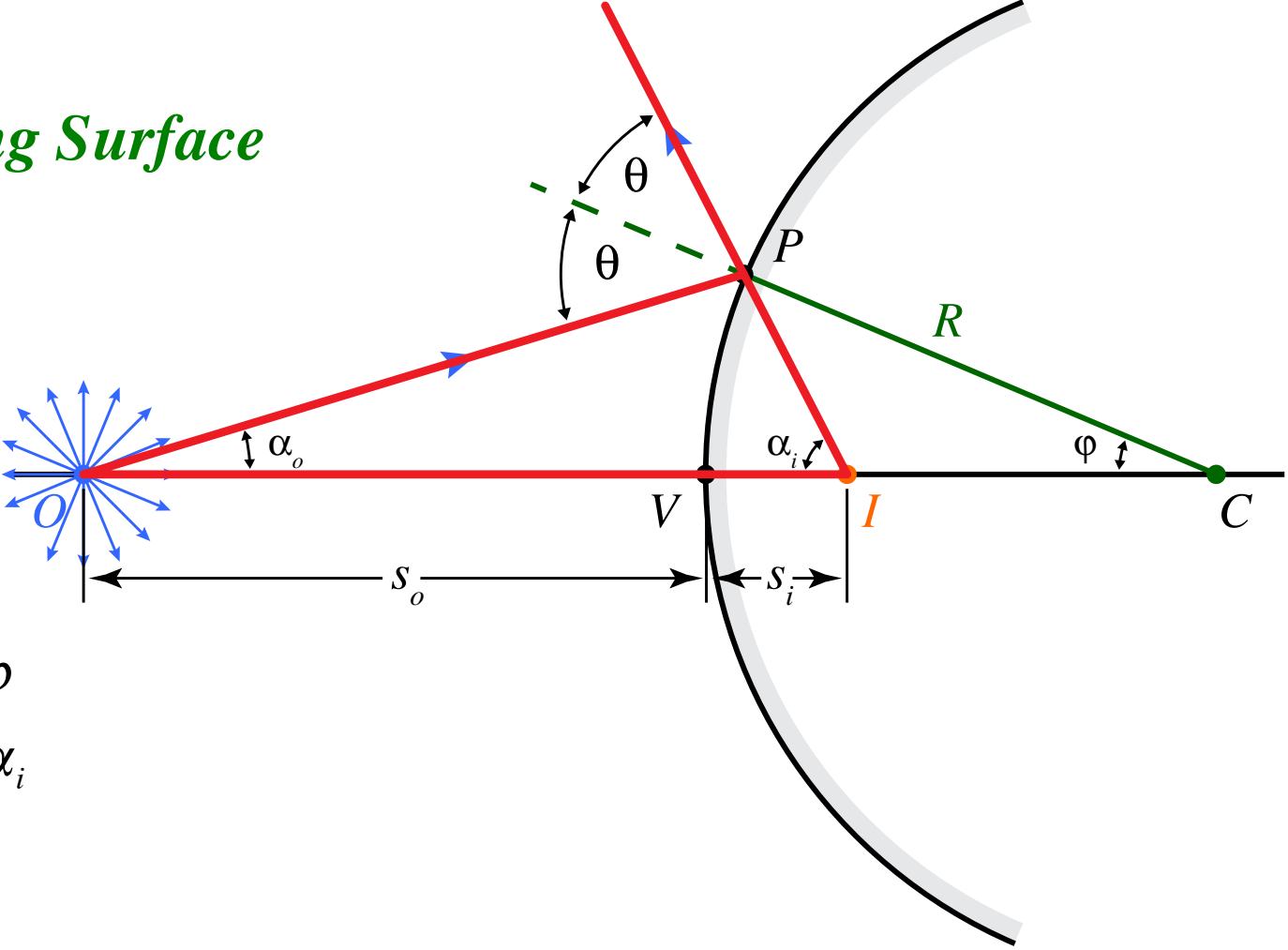


*Convex Reflecting Surface*



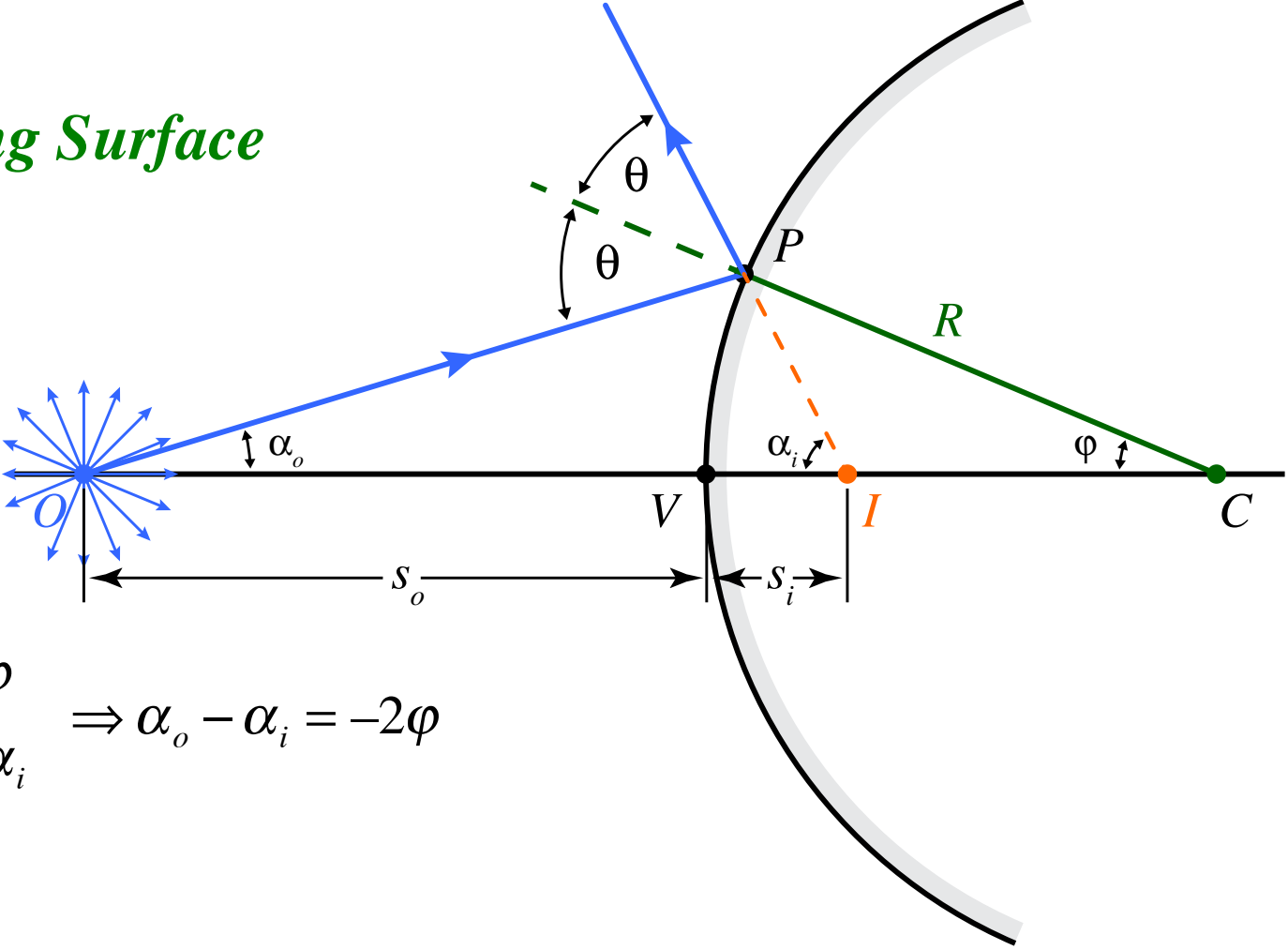
$$\theta = \alpha_o + \varphi$$

# Convex Reflecting Surface



$$\theta = \alpha_o + \phi$$
$$2\theta = \alpha_o + \alpha_i$$

# Convex Reflecting Surface

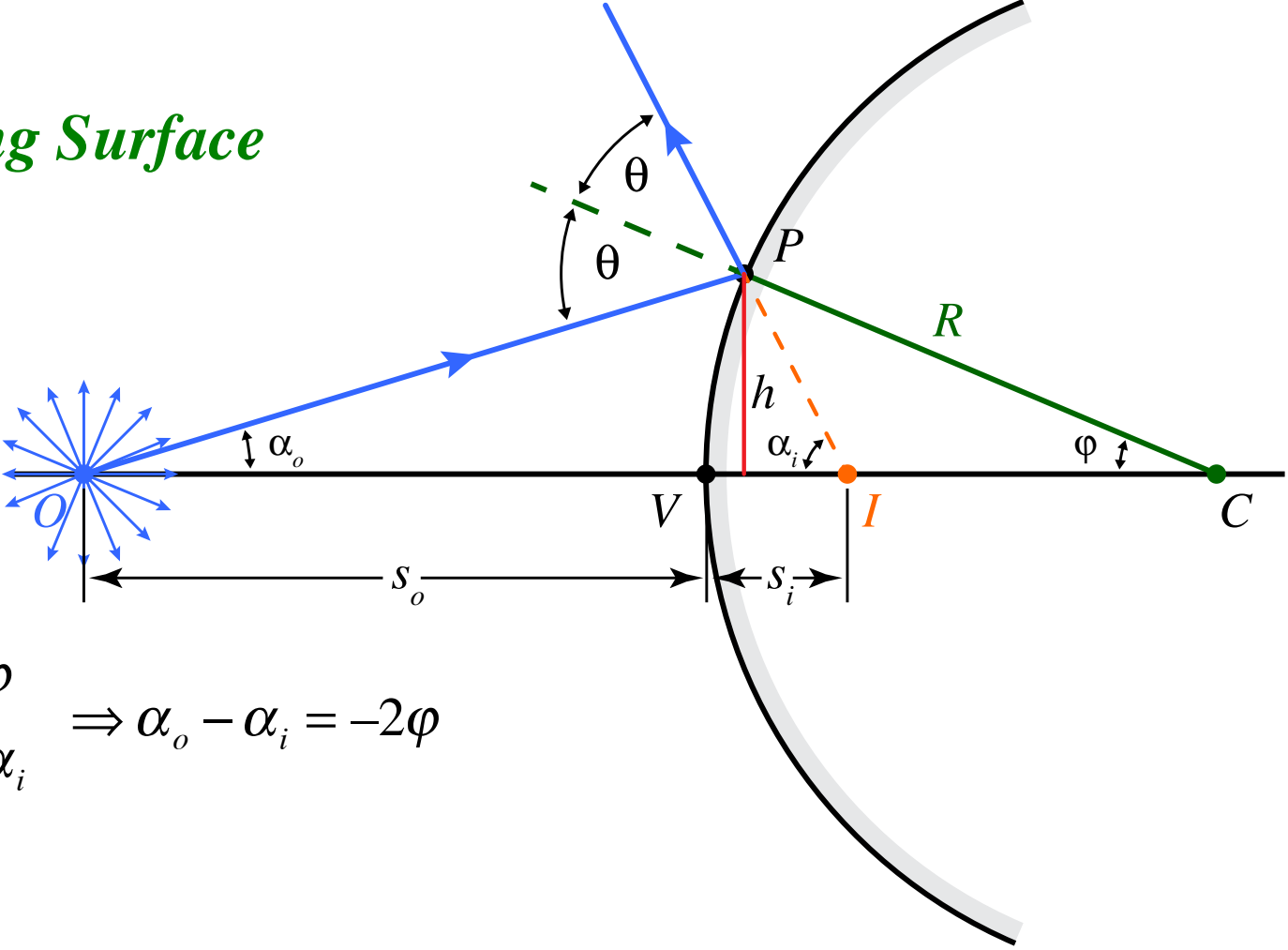


$$\theta = \alpha_o + \phi$$

$$2\theta = \alpha_o + \alpha_i \Rightarrow \alpha_o - \alpha_i = -2\phi$$



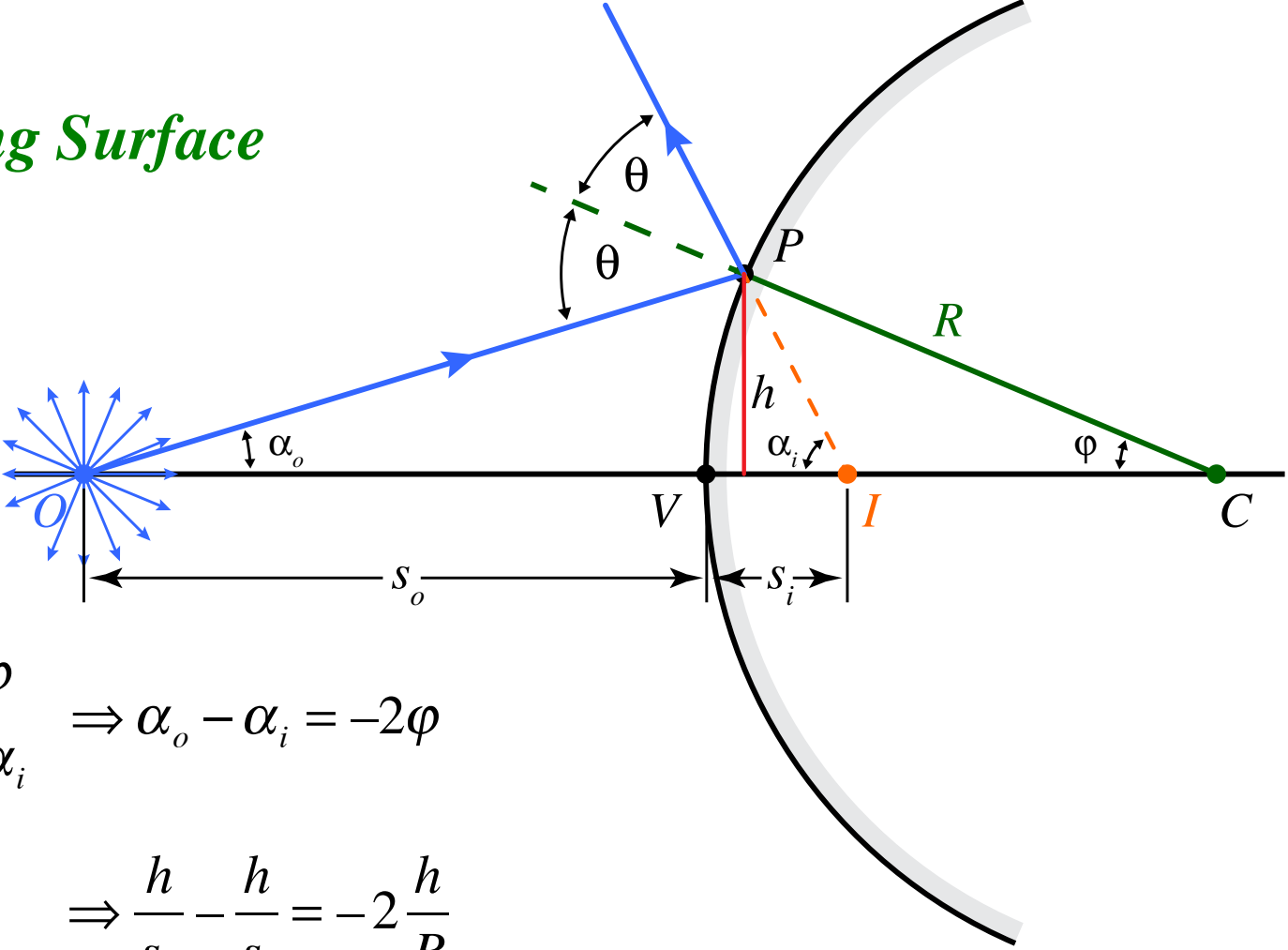
# Convex Reflecting Surface



$$\theta = \alpha_o + \phi$$

$$2\theta = \alpha_o + \alpha_i \Rightarrow \alpha_o - \alpha_i = -2\phi$$

# Convex Reflecting Surface

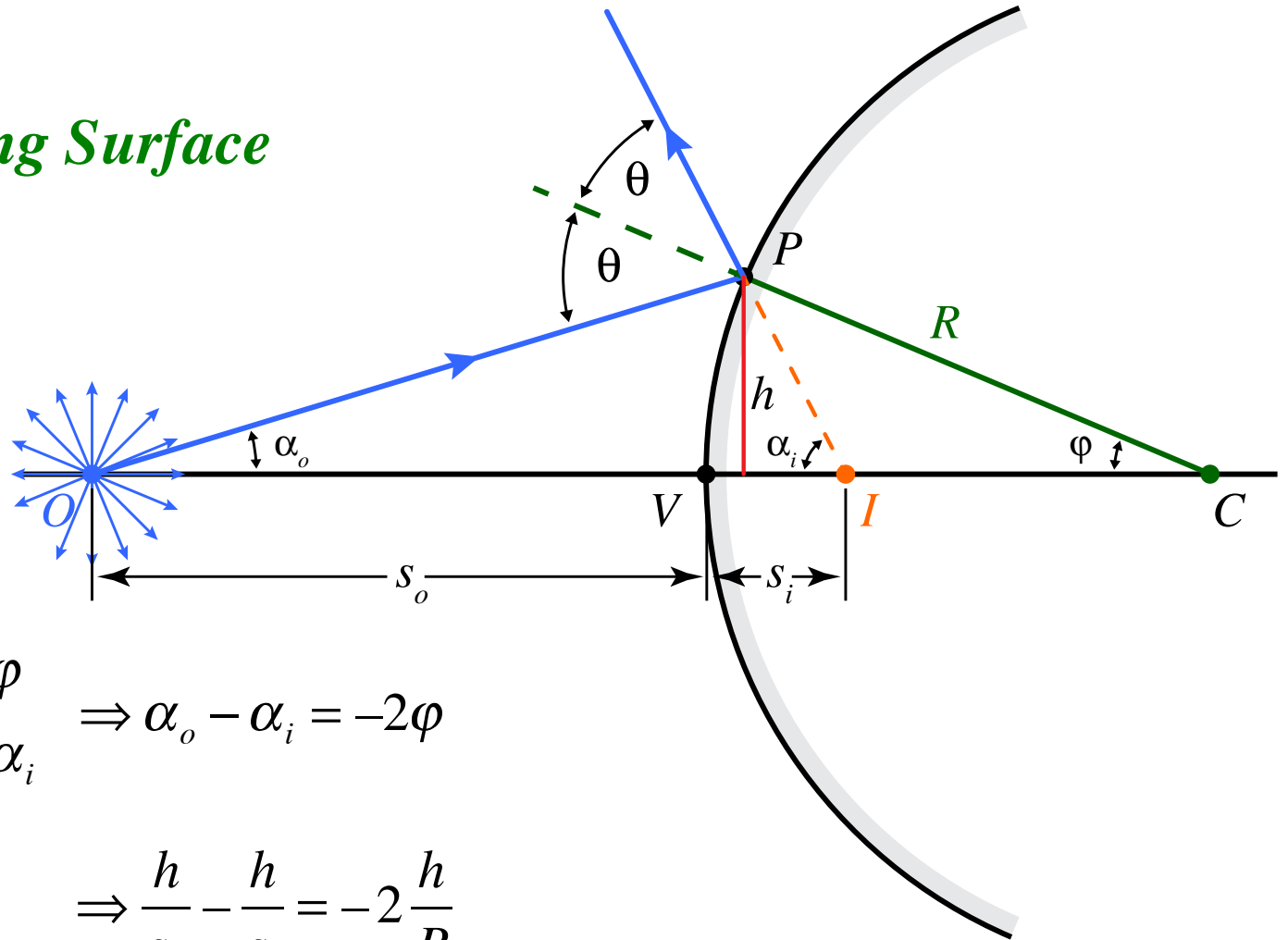


$$\theta = \alpha_o + \phi \Rightarrow \alpha_o - \alpha_i = -2\phi$$

$$2\theta = \alpha_o + \alpha_i$$

$$\Rightarrow \frac{h}{s_o} - \frac{h}{s_i} = -2 \frac{h}{R}$$

## Convex Reflecting Surface



$$\begin{aligned}\theta &= \alpha_o + \varphi \\ 2\theta &= \alpha_o + \alpha_i\end{aligned}\quad \Rightarrow \quad \alpha_o - \alpha_i = -2\varphi$$

$$\Rightarrow \frac{h}{s_o} - \frac{h}{s_i} = -2\frac{h}{R}$$

$$\Rightarrow \frac{1}{s_o} - \frac{1}{s_i} = -\frac{2}{R}$$

## *Convex Reflecting Surface*

$$\frac{1}{s_o} - \frac{1}{s_i} = -\frac{2}{R}$$

## *Concave Reflecting Surface*

$$\frac{1}{s_o} + \frac{1}{s_i} = +\frac{2}{R}$$

*Let's standardize on one equation*

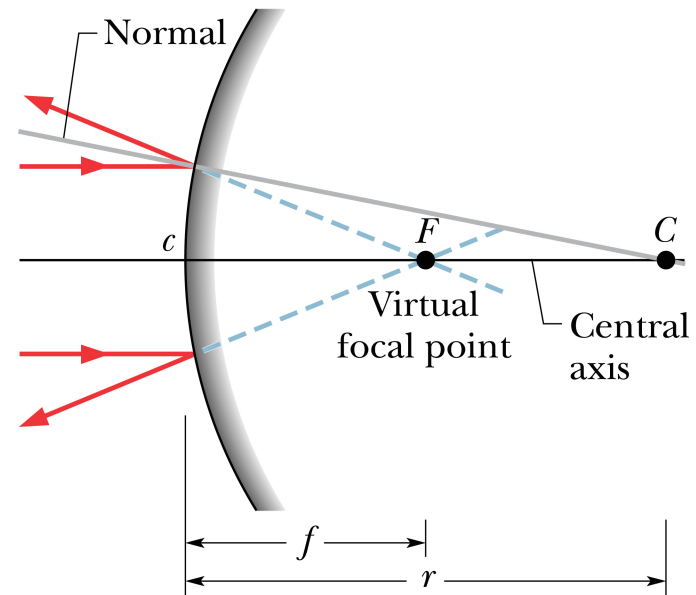
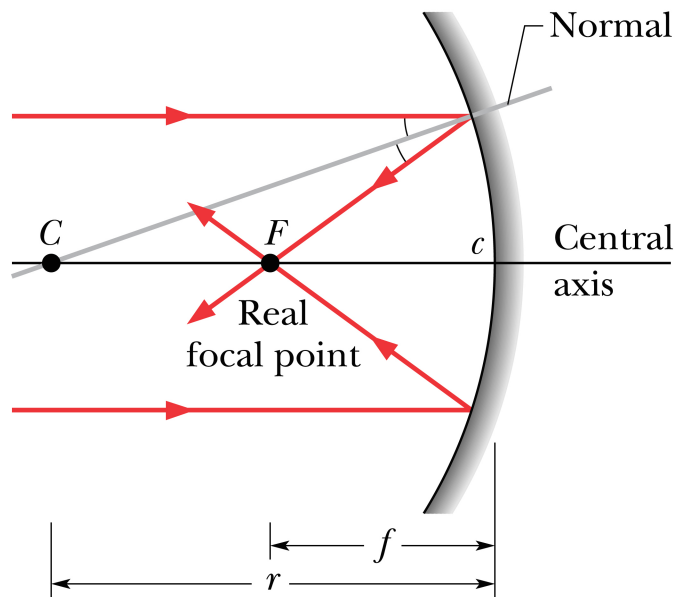
$$\frac{1}{s_o} + \frac{1}{s_i} = -\frac{2}{R}$$

*and adopt a sign convention (rays coming from the left)*

- Object,  $s_o$  :
- + when  $O$  is to the left of  $V$  (real object)
  - when  $O$  is to the right of  $V$  (virtual object)
- Image,  $s_i$  :
- + when  $I$  is to the left of  $V$  (real image)
  - when  $I$  is to the right of  $V$  (virtual image)
- Radius,  $R$  :
- when  $C$  is to the left of  $V$  (concave surface)
  - + when  $C$  is to the right of  $V$  (convex surface)

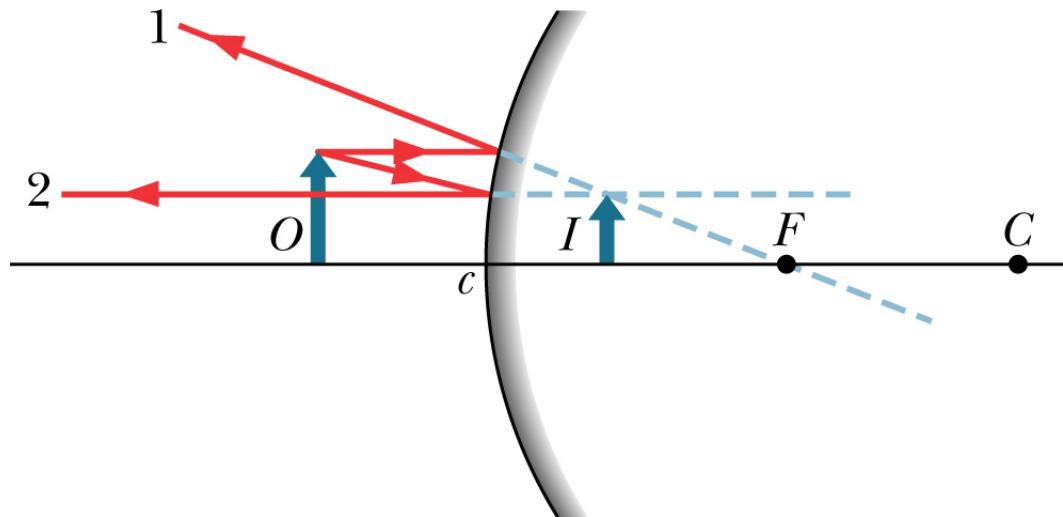
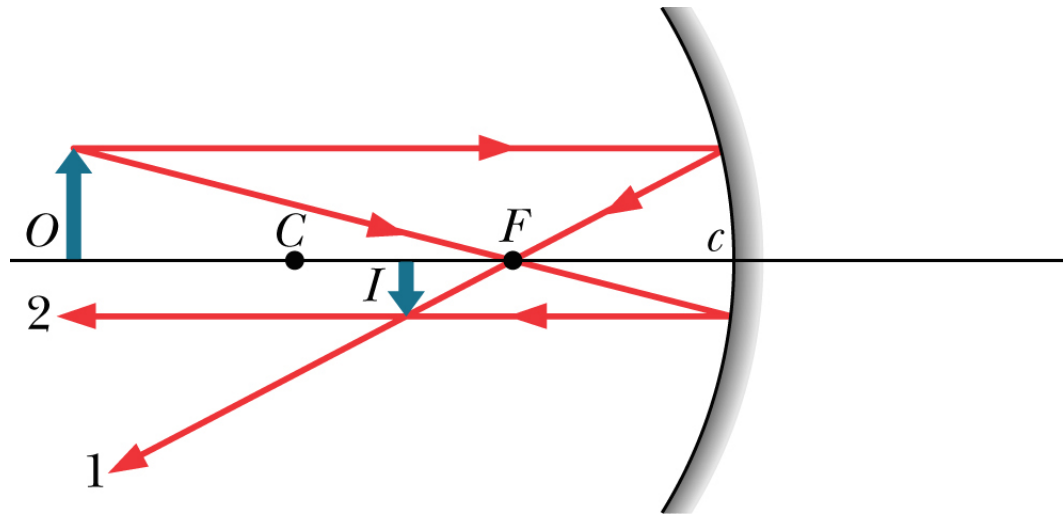
*For an object at infinity*

$$s_o = \infty \Rightarrow \frac{1}{\infty} + \frac{1}{s_i} = -\frac{2}{R} \Rightarrow s_i = -\frac{R}{2} = f$$

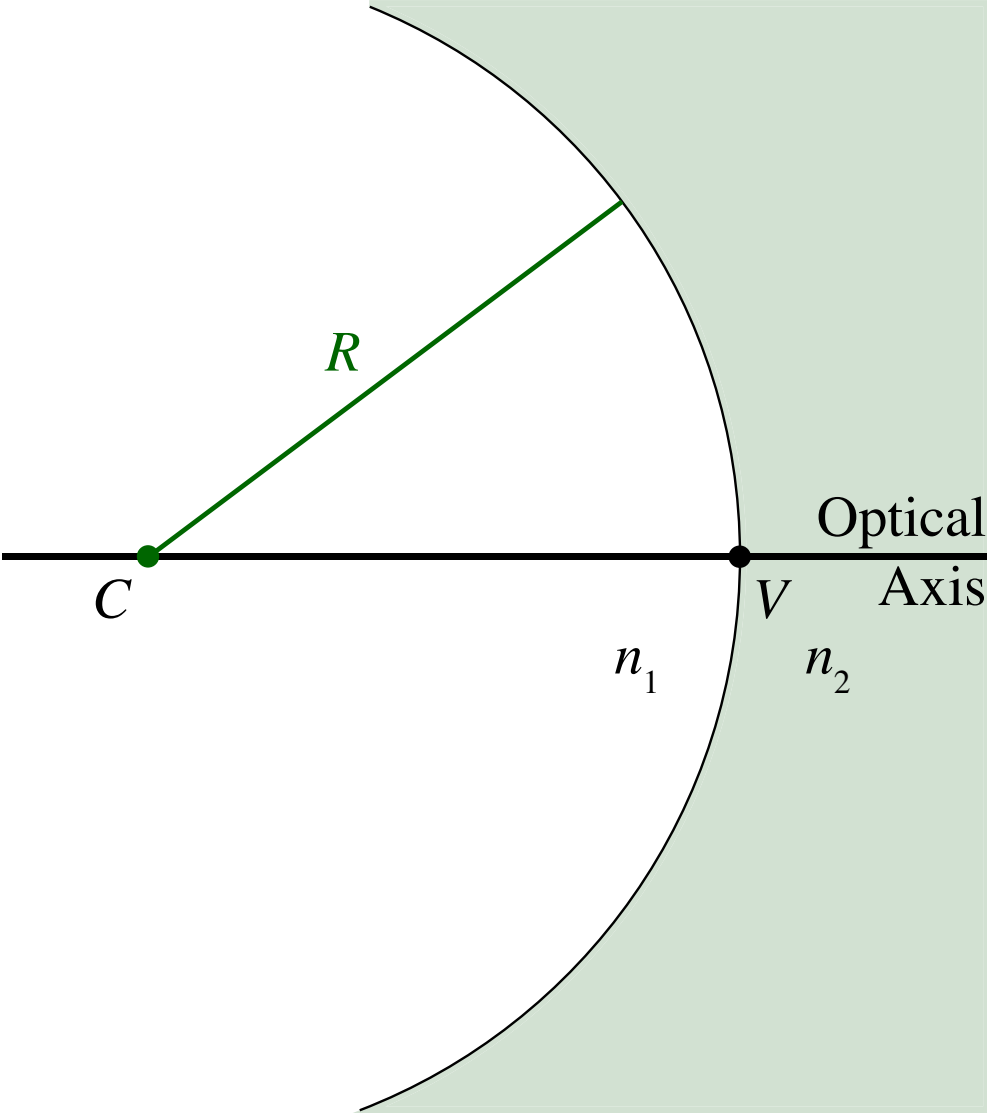


*$f$ : focal length of the mirror*

*Knowing  $f$  is useful for drawing ray diagrams to find the image*

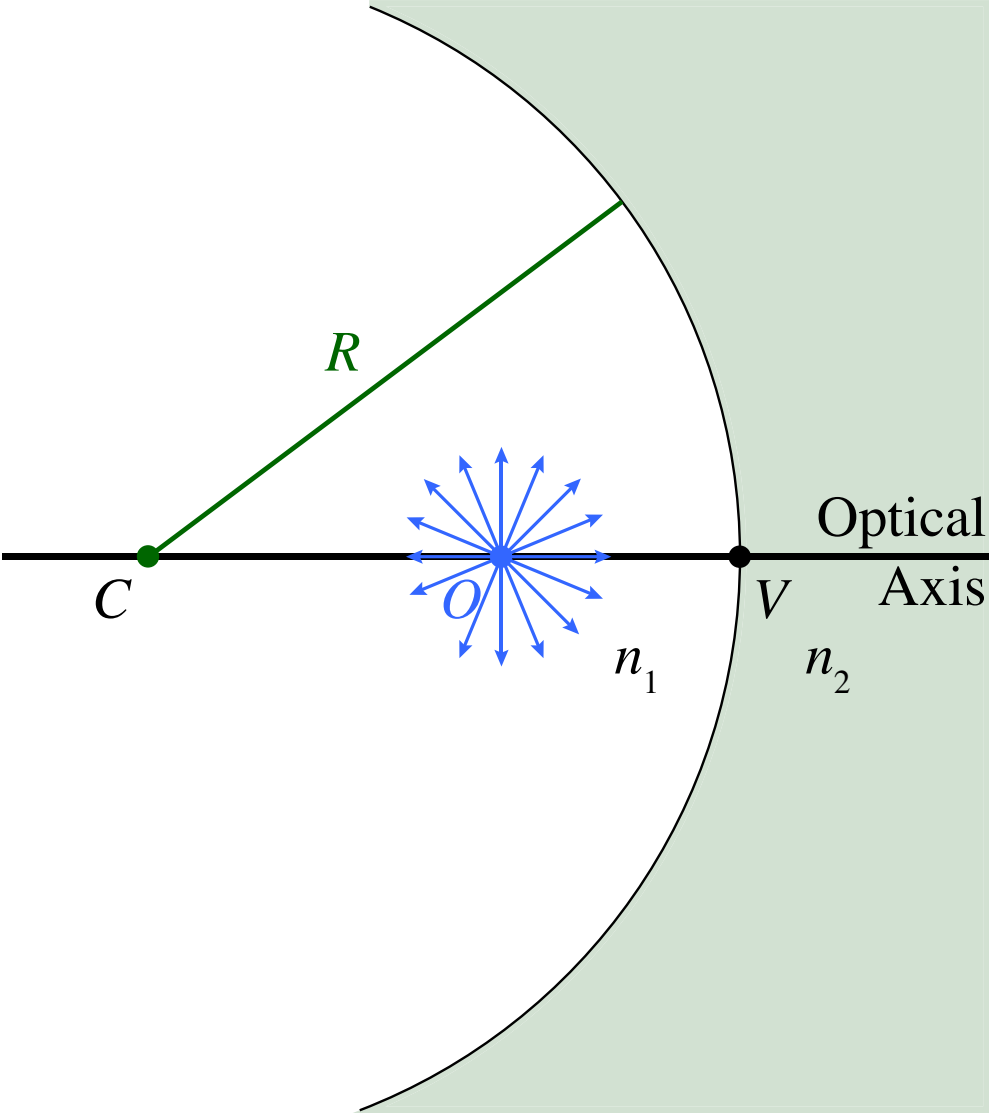


*Concave Refracting Surface*

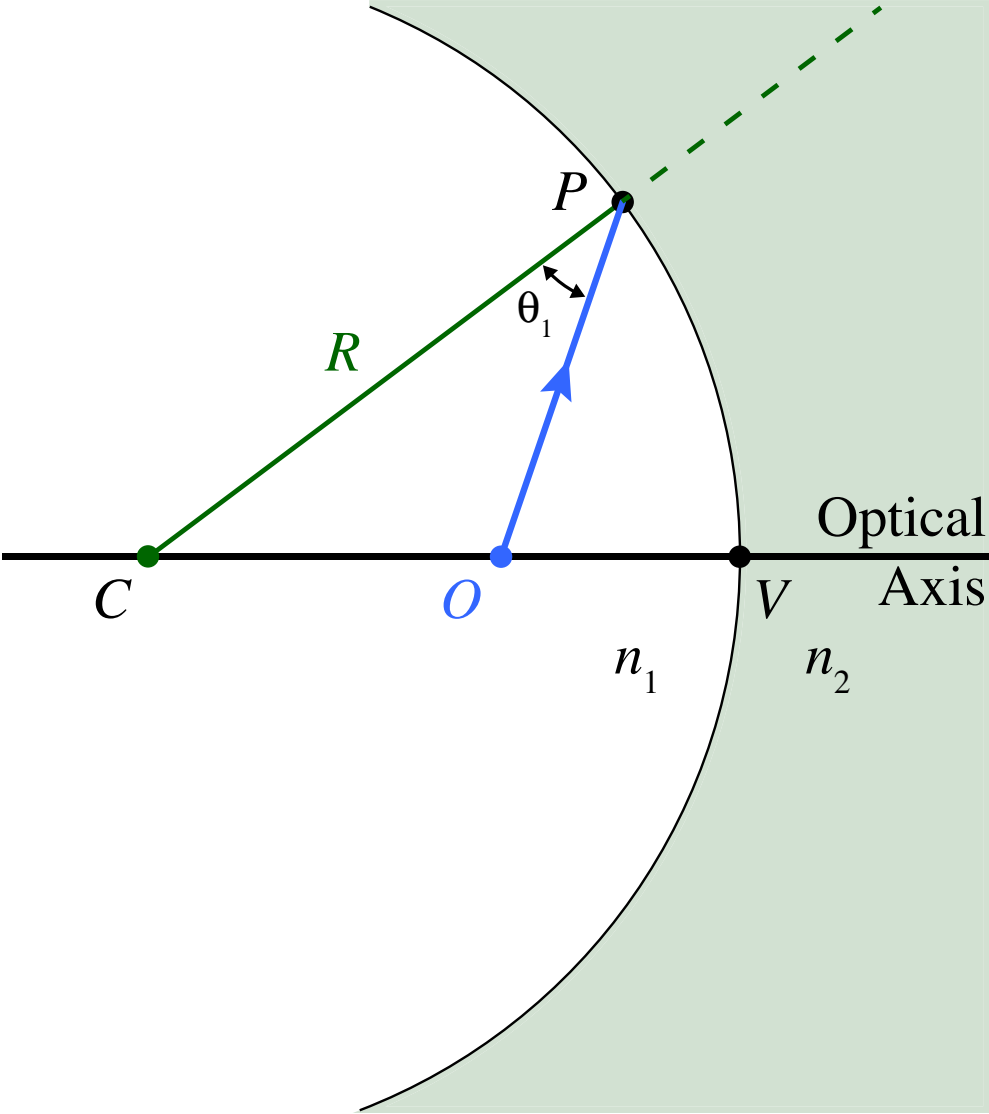




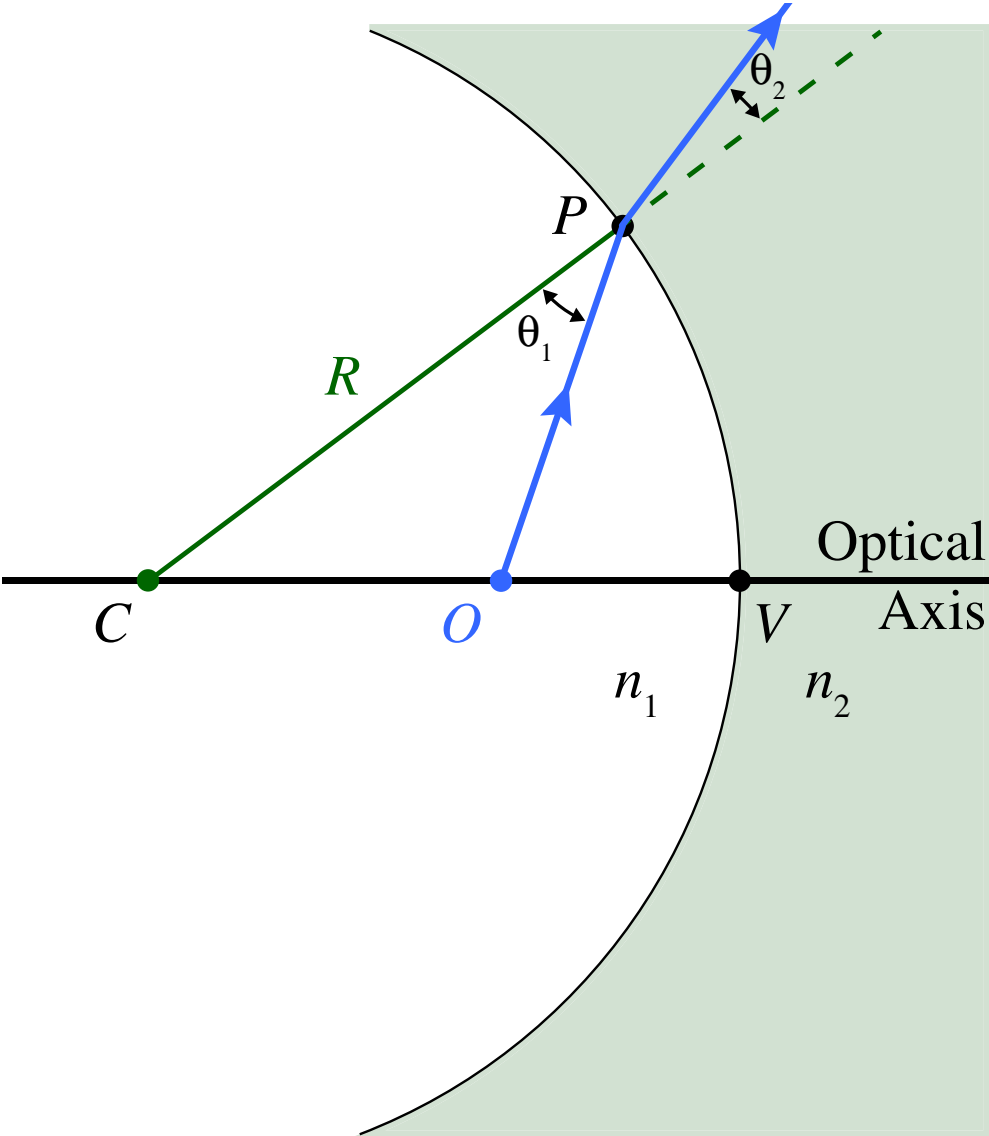
*Concave Refracting Surface*



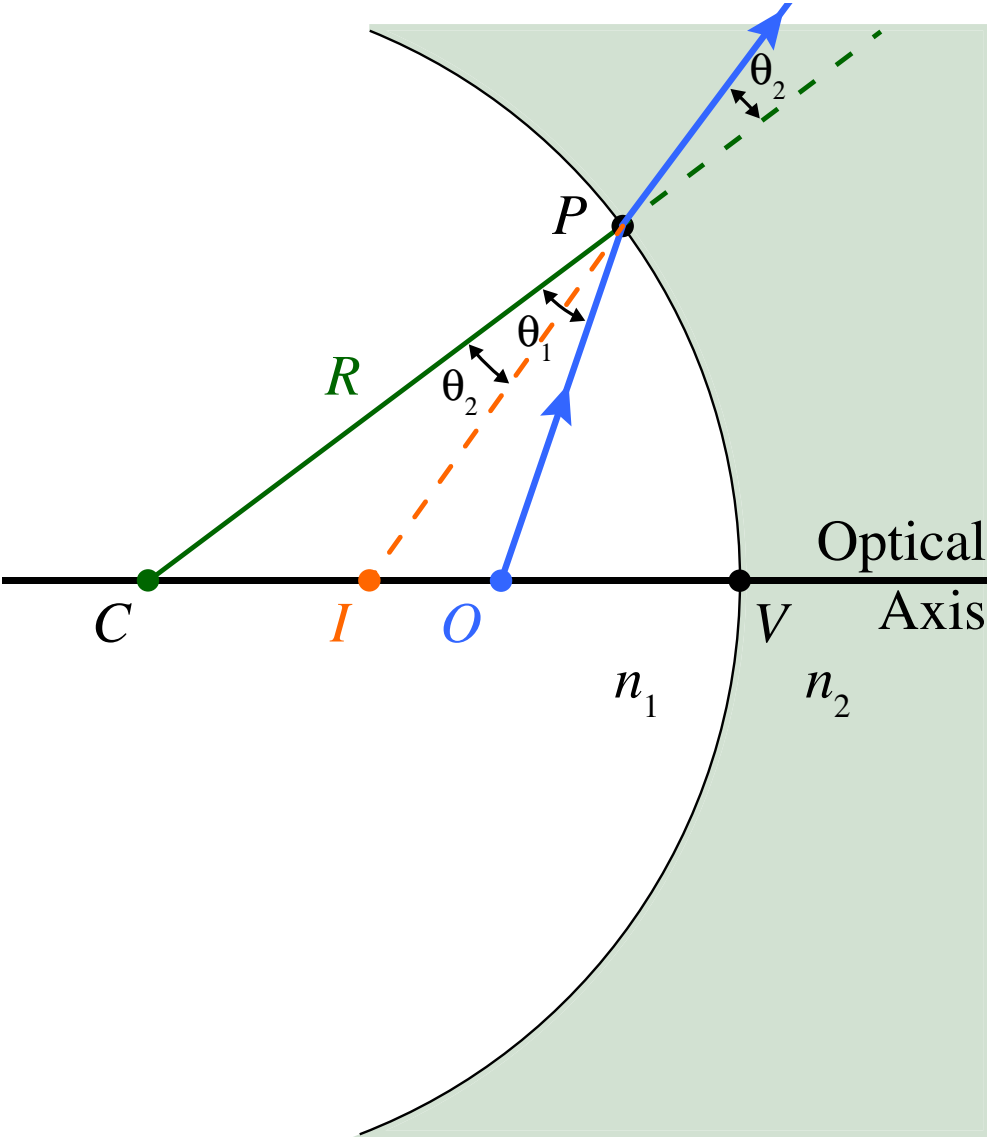
*Concave Refracting Surface*



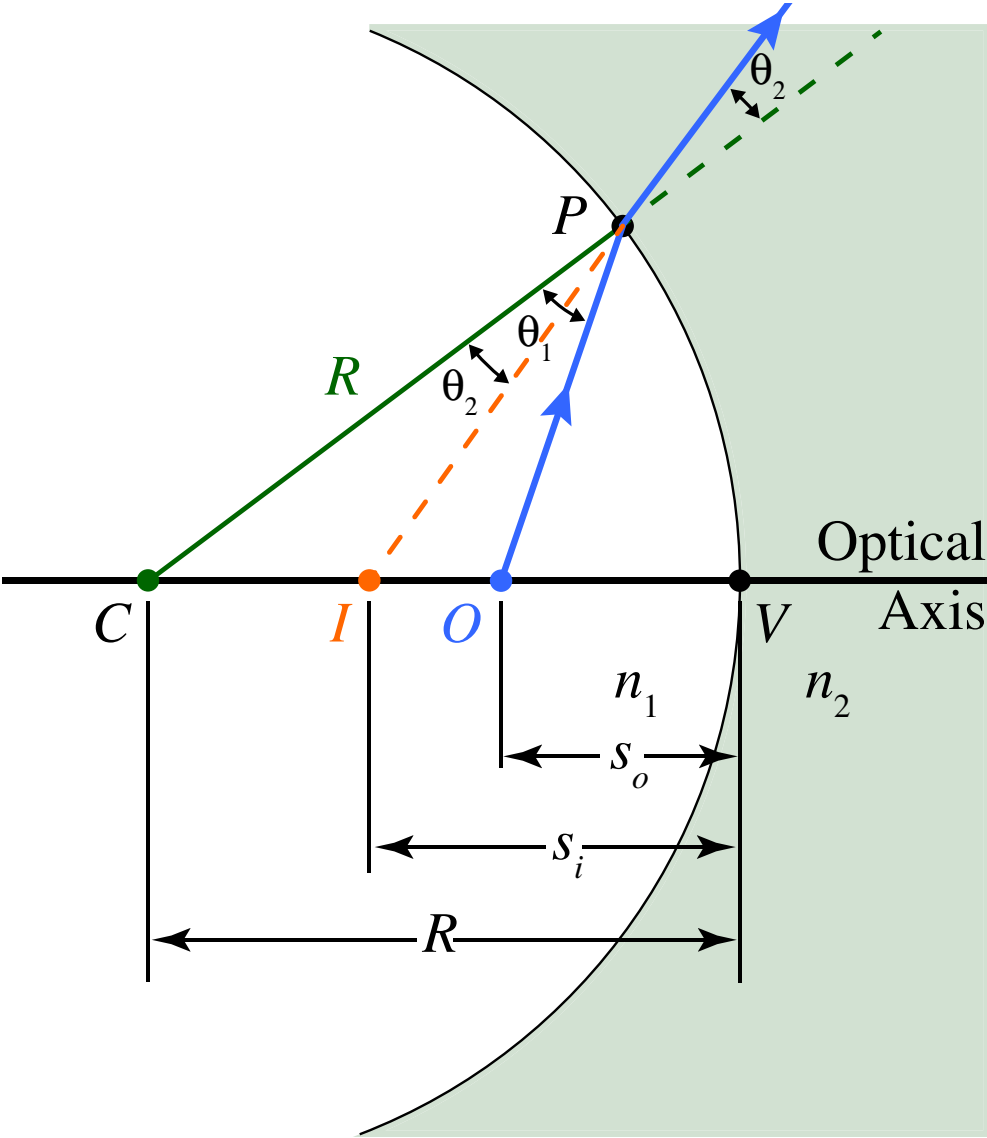
*Concave Refracting Surface*



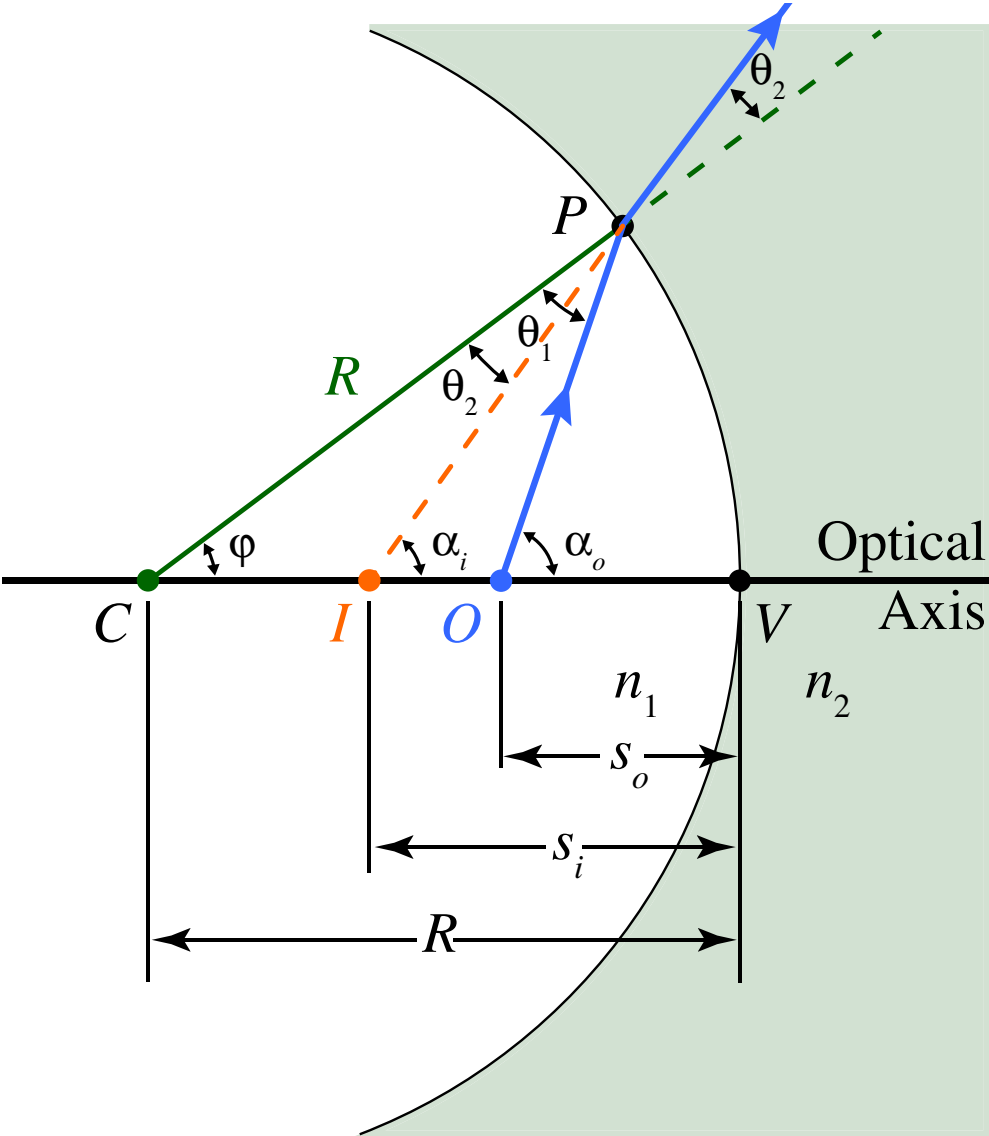
*Concave Refracting Surface*



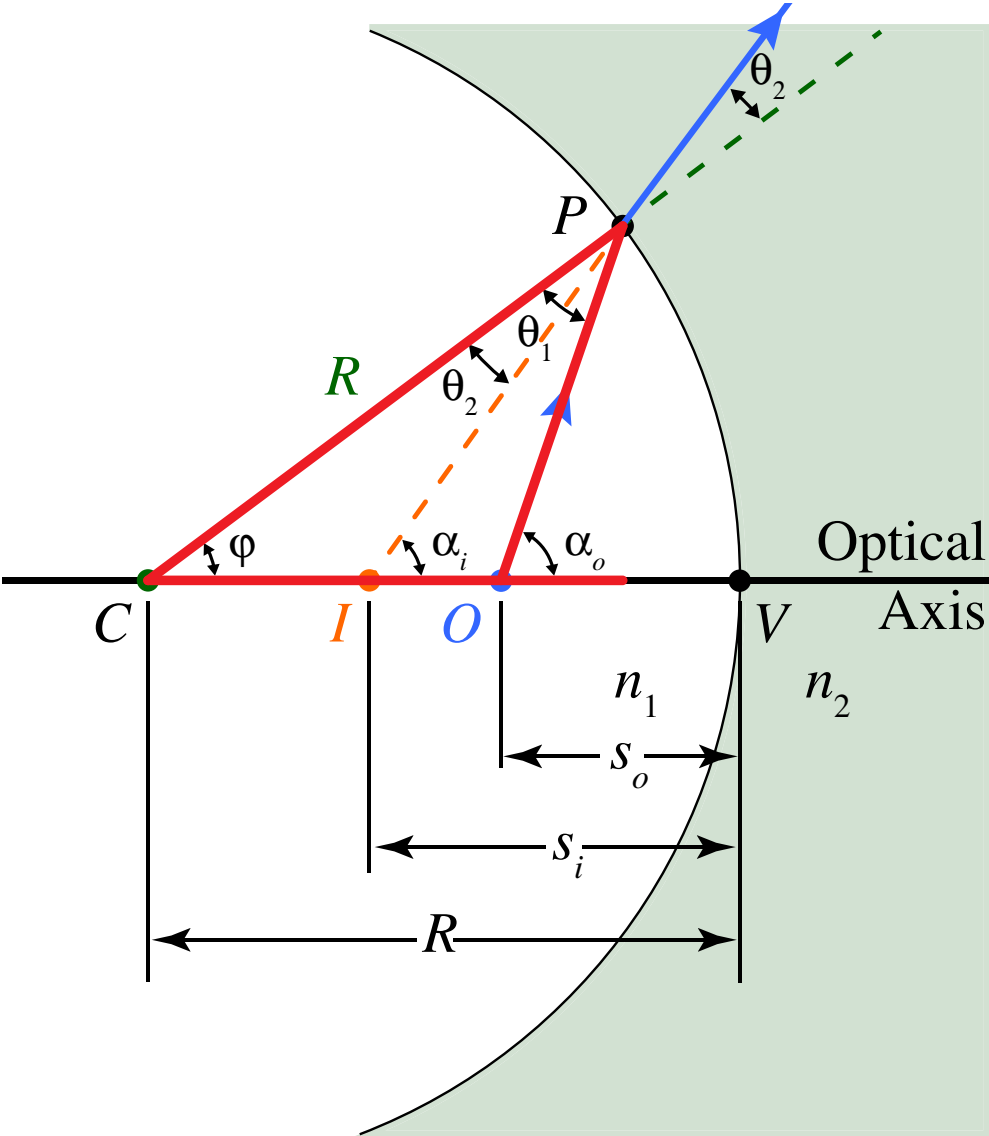
*Concave Refracting Surface*



*Concave Refracting Surface*



# Concave Refracting Surface

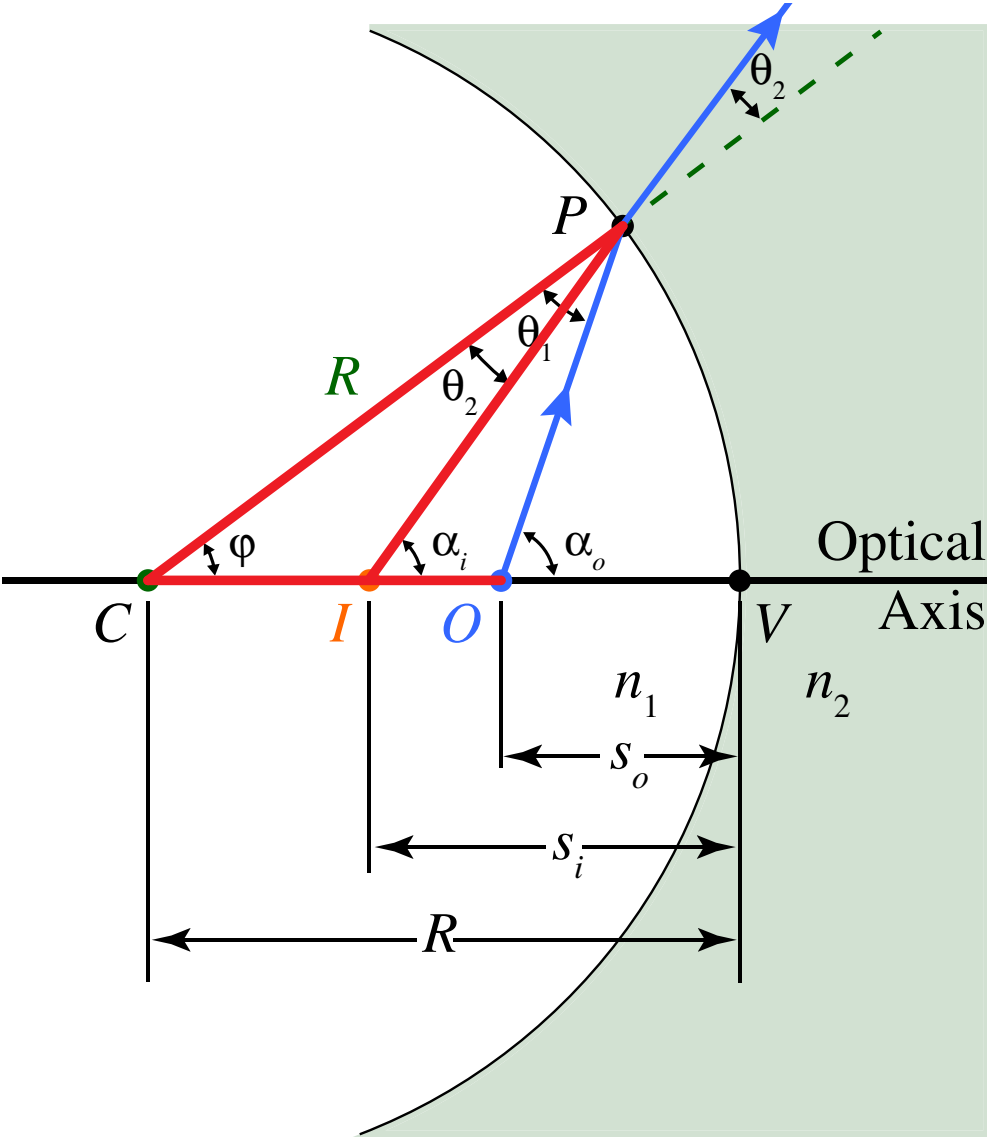


$$\alpha_o = \varphi + \theta_1$$

# Concave Refracting Surface

$$\alpha_o = \varphi + \theta_1$$

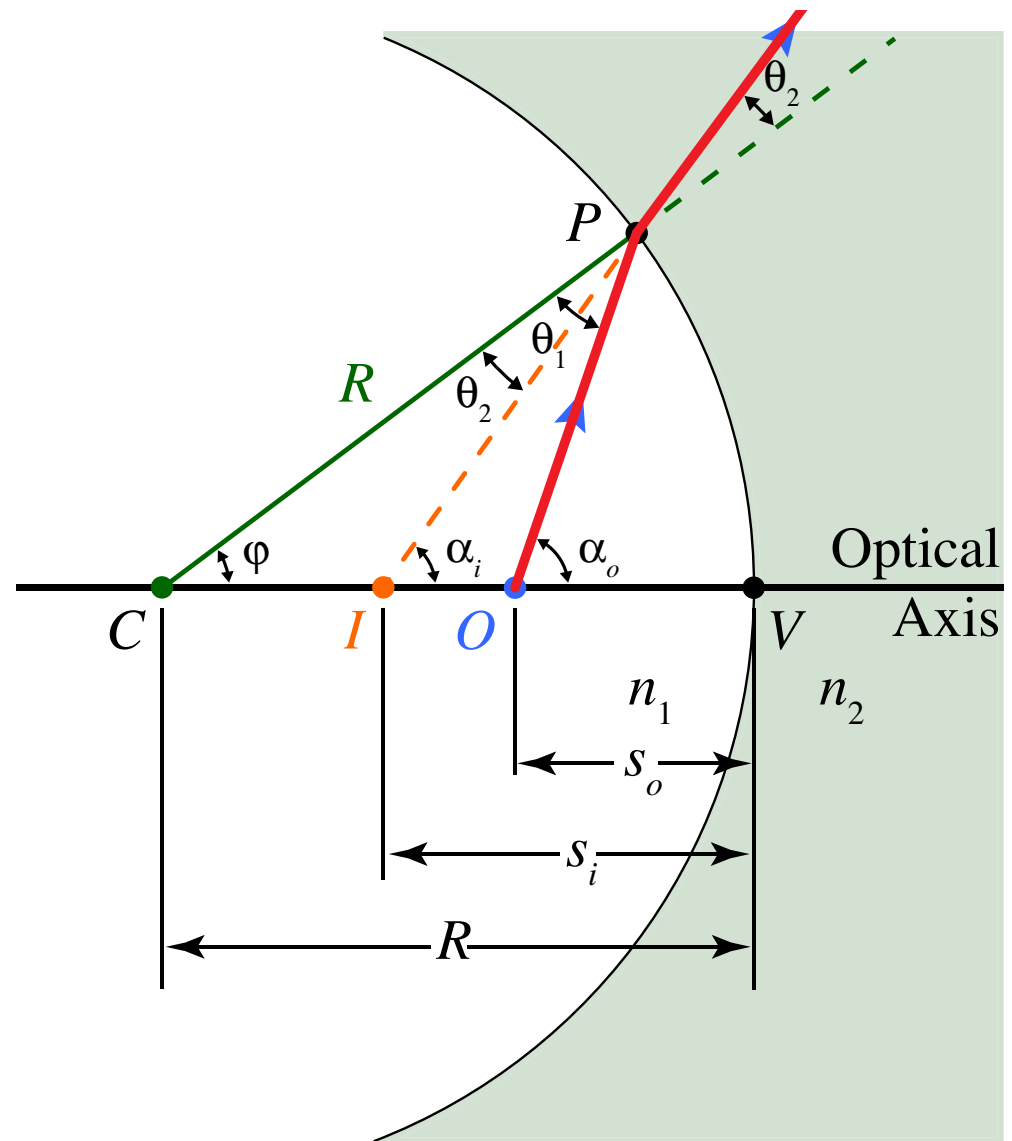
$$\alpha_i = \varphi + \theta_2$$





## Concave Refracting Surface

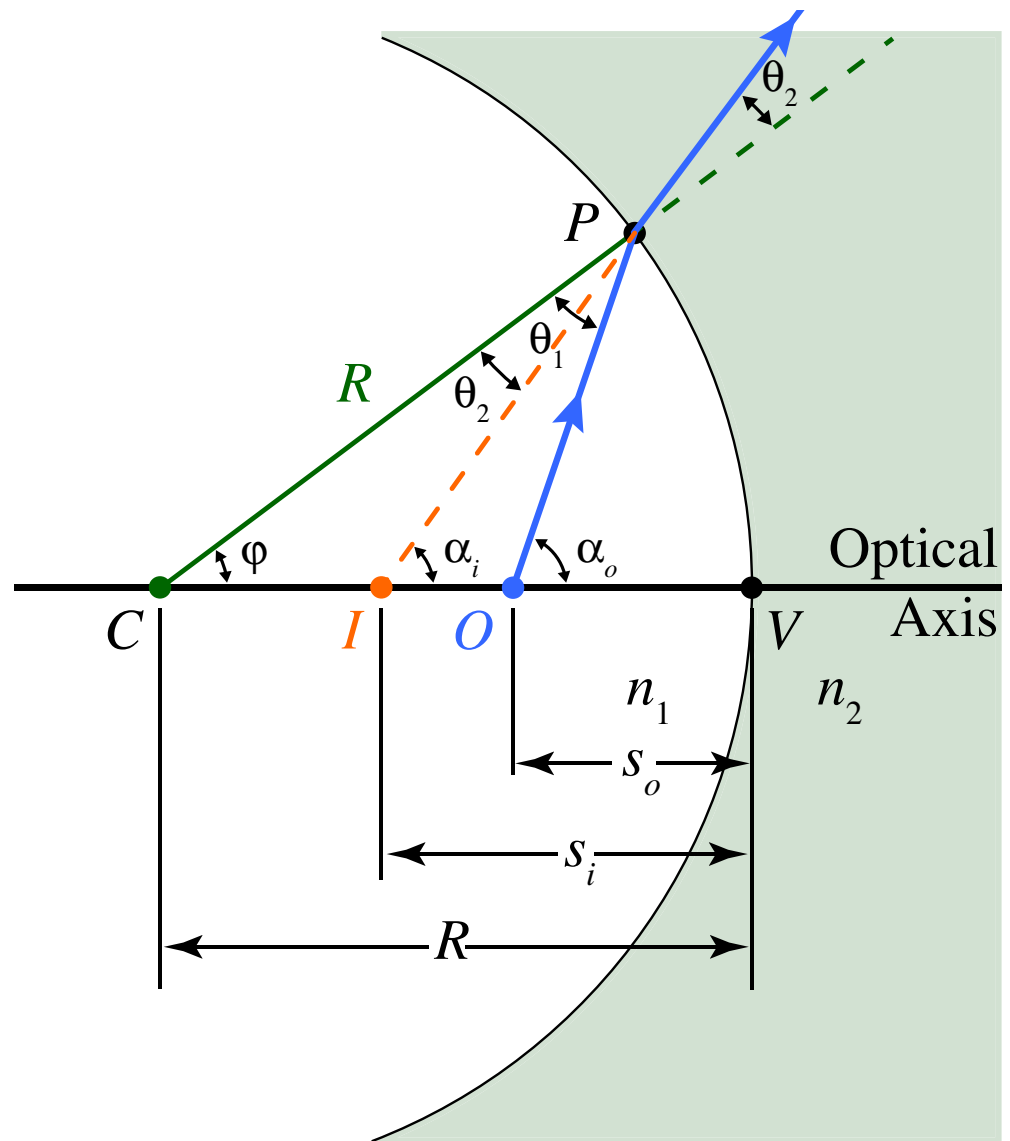
$$\alpha_o = \varphi + \theta_1$$
$$\alpha_i = \varphi + \theta_2$$
$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$



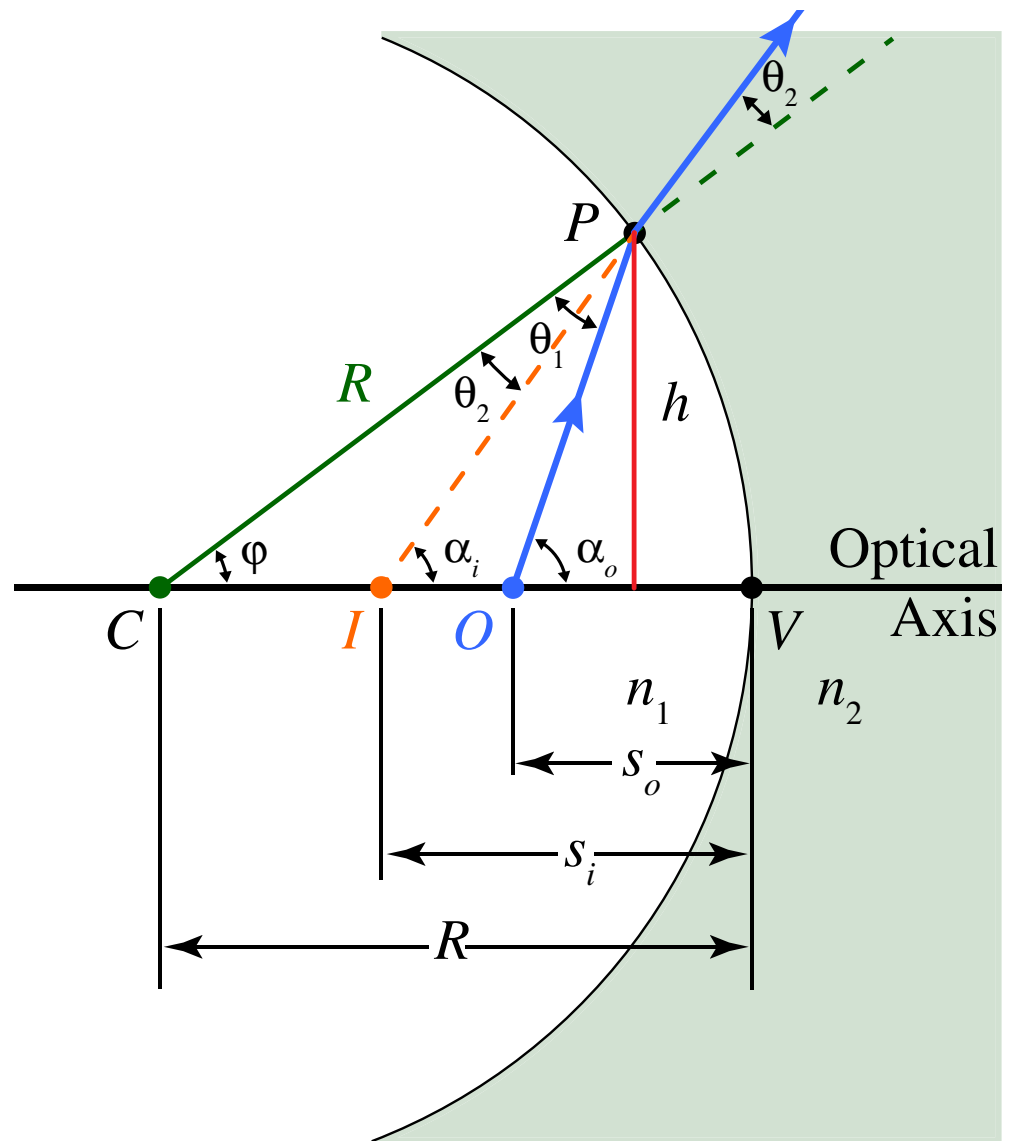
## Concave Refracting Surface

$$\alpha_o = \varphi + \theta_1$$
$$\alpha_i = \varphi + \theta_2$$
$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\Rightarrow n_1 (\alpha_o - \varphi) = n_2 (\alpha_i - \varphi)$$



## Concave Refracting Surface



$$\alpha_o = \varphi + \theta_1$$

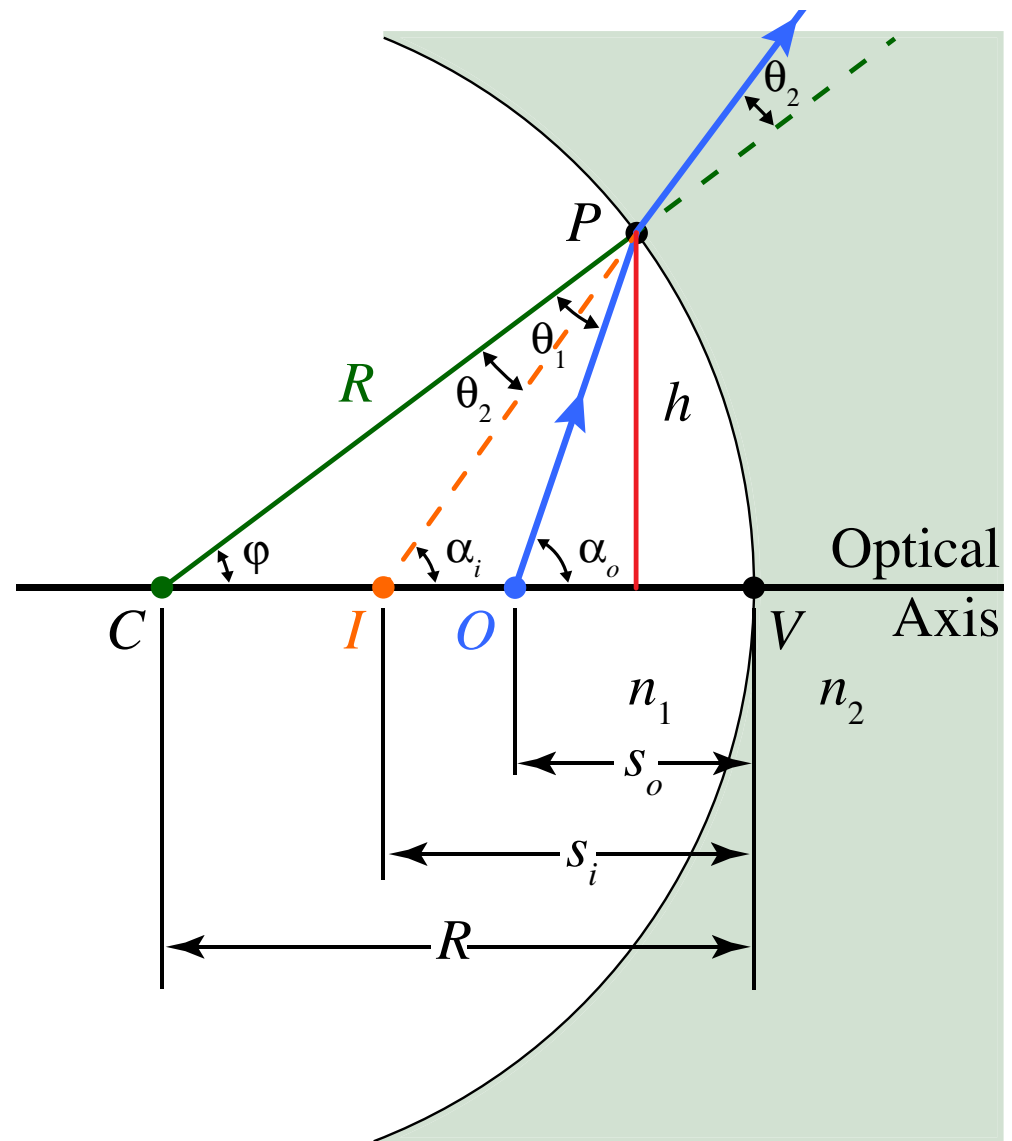
$$\alpha_i = \varphi + \theta_2$$

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\Rightarrow n_1 (\alpha_o - \varphi) = n_2 (\alpha_i - \varphi)$$

$$\Rightarrow n_1 \left( \frac{h}{s_o} - \frac{h}{R} \right) = n_2 \left( \frac{h}{s_i} - \frac{h}{R} \right)$$

## Concave Refracting Surface



$$\alpha_o = \varphi + \theta_1$$

$$\alpha_i = \varphi + \theta_2$$

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\Rightarrow n_1 (\alpha_o - \varphi) = n_2 (\alpha_i - \varphi)$$

$$\Rightarrow n_1 \left( \frac{h}{s_o} - \frac{h}{R} \right) = n_2 \left( \frac{h}{s_i} - \frac{h}{R} \right) \Rightarrow \frac{n_1}{s_o} - \frac{n_2}{s_i} = \frac{n_1 - n_2}{R}$$

## *Concave Refracting Surface*

$$\frac{n_1}{s_o} - \frac{n_2}{s_i} = \frac{n_1 - n_2}{R}$$

## *Convex Refracting Surface*

$$\frac{n_1}{s_o} + \frac{n_2}{s_i} = -\frac{n_1 - n_2}{R}$$

*Again, let's standardize on one equation*

$$\frac{n_1}{s_o} + \frac{n_2}{s_i} = \frac{n_2 - n_1}{R}$$

*and adopt a sign convention*

real objects	}	+ distances
real images		
convex surface		
virtual objects	}	- distances
virtual images		
concave surface		