

Linear, 2nd order, non-homogeneous differential equation with constant coefficients.

$$a \frac{d^2 y(x)}{dx^2} + b \frac{dy(x)}{dx} + c y(x) = f(x)$$

The solutions are given by:

$$y(x) = y_p(x) + y_c(x)$$

where $y_c(x) \equiv$ complementary solution to the homogeneous equation.

To find $y_p(x)$, we guess at a solution. The guess we make will depend on $f(x)$.

$f(x)$	$y_p(x)$
$P_n(x) = a_n x^n + a_{n-1} x^{n-1} + \cdots + a_1 x + a_0$	$x^s (A_n x^n + A_{n-1} x^{n-1} + \cdots + A_1 x + A_0)$
$P_n(x) e^{\alpha x}$ ($\alpha =$ real or complex)	$x^s (A_n x^n + A_{n-1} x^{n-1} + \cdots + A_1 x + A_0) e^{\alpha x}$
$P_n(x) e^{\alpha x} \cos(kx)$ or $P_n(x) e^{\alpha x} \sin(kx)$	$x^s \left[(A_n x^n + \cdots + A_0) e^{\alpha x} \cos(kx) + (B_n x^n + \cdots + B_0) e^{\alpha x} \sin(kx) \right]$

Here s is the smallest nonnegative integer ($s = 0, 1, 2$) which will insure that no term in $y_p(x)$ is a solution of the corresponding homogeneous equation.